

Mathematical Modeling: Corruption Case- IV of the Society of India

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Abstract:

In this paper we have to study on the problem of 'Corruption' in different ways by using mathematical modeling. In this connection we have found the formula that is Mathematical corruption model for measuring corruption in the society of the country. Therefore we have taken some illustrations for measuring the corruption in the society for case-IV.

Keywords: mathematical thinking, corruption mentality, modeling, applied.

I. INTRODUCTION:

The Mathematical Results for measuring "Corruption" in the society. These mathematical results are as follows:

i. Mathematical Corruption Model (or MC Model) Formula:

$$C = C_0(K + 1)^t$$

ii. Mathematical Corruption-Development Model (or MCD Model) Formula:

$$D(C) = D(0) [1 + K]^C$$

iv. Mathematical E-virus Constant Model with Related Time (MEVC Model) Formula:

$$K = \left[\frac{C(t)}{C(0)} \right]^{\frac{1}{t}} - 1, -1 < K < 1$$

v. Mathematical E-virus Constant Model with Related Corruption (MEVC Model) Formula:

$$K = \left[\frac{D(C)}{D(0)} \right]^{\frac{1}{C}} - 1, -1 < K < 1$$

Note that if the value of K is more than 1 then we choose or take the value approximately to 1 but not equal to 1.

II. METHODOLOGY:

We have to use the seven steps of mathematical modeling process for solving the problem of corruption in the society of any country of the world. Also we can represent mathematical modeling process in the form "Visual". Therefore it is known as visual mathematical modeling process. It is as follows:

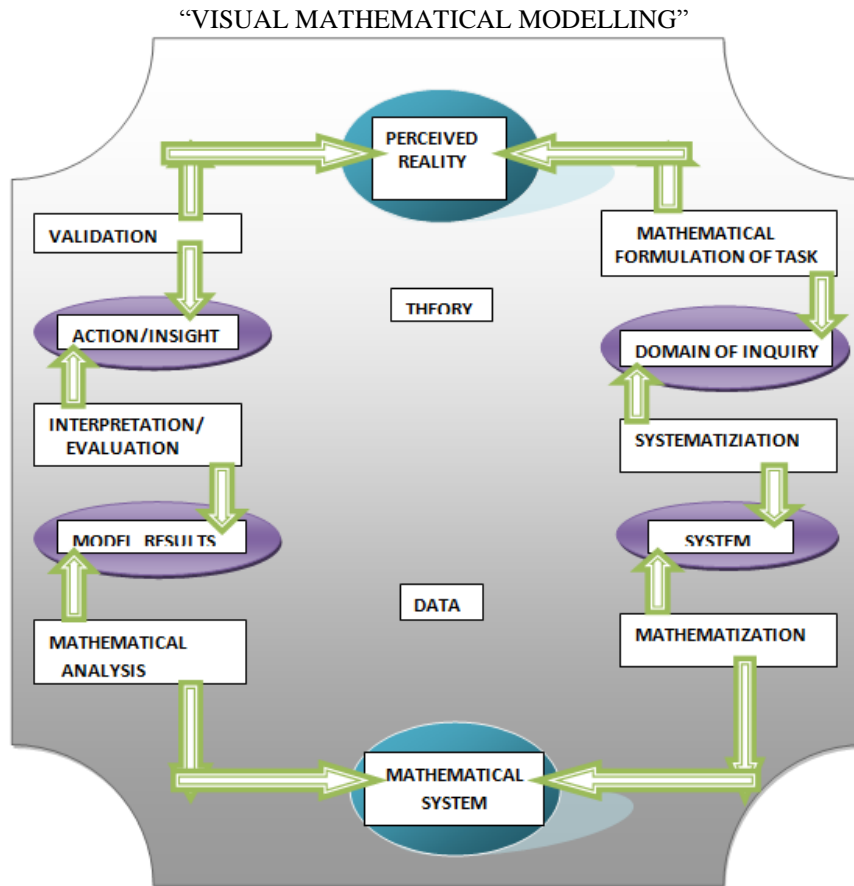


Fig-1: A Visual representation of the Mathematical Modeling process
 Mathematical modeling means “Translation from real world problems into Mathematics world.”

III. SOME ILLUSTRATIONS FOR MEASURING CORRUPTION IN THE SOCIETY:

3. Mathematical Corruption grows in various fields of the society (general) for case-IV:

We assume that corruption was 1.00 % of total population 35 crore that is 0.3500 crore on 15 August, 1957. Therefore at MEV constant $K=0$. When $t=0$, $C(0) = C_0 = 0.3500$ crore and when $t= 10$ years, $C(t)$ depends on MEV constant. We know that MEV constant formula,

$$\text{Therefore, } K = \left[\frac{C(t)}{C(0)} \right]^{\frac{1}{t}} - 1$$

Putting in Mathematical corruption model formula(i). it is of the form,

$$\text{Therefore, } C = C_0(K + 1)^t$$

$$C = 0.3500 \times \left[\frac{C(t)}{C(0)} \right]^{\frac{t}{10}} \quad \text{----- (i)}$$

Where K is known as MEV constant. So we take the various values of MEV constant K . It lies between 0 and 1. Such values are 0, 0.20, 0.40, 0.60, 0.80 and 0.9988.

Case-I: we take $K=0$ and $t= 10$ years then from (vi), $C= C_0 = 0.3500$ crore

Therefore, $C = 0.3500$ crore

Case-II: when, we take $K=0.20$ and MM period $t = 10$ years, $C(t) = 0.4200$ crore then

from (i), Therefore, $C = 0.3500 \times \left[\frac{0.4200}{0.3500} \right]^{\frac{t}{10}} \quad \text{----- (ii)}$

When MM period $t = 10$ years from base that is 15 August 1947. What is C ?

Therefore, $C = 0.3500 \times [1.20]^{\frac{10}{10}}$
 $C = 0.3500 \times 1.20$
 $C = 0.4200$ crore

When MM period $t = 20$ years from base that is 15 August 1947. What is C ?

Therefore, $C = 0.3500 \times [1.20]^{\frac{20}{10}}$
 $C = 0.3500 \times 1.44$
 $C = 0.5040$ crore

When MM period $t = 30$ years from base that is 15 August 1947. What is C ?

Therefore, $C = 0.3500 \times [1.20]^{\frac{30}{10}}$
 $C = 0.3500 \times 1.728$
C = 0.6048 crore

When MM period t = 40 years from base that is 15 August 1947. What is C ?

Therefore, $C = 0.3500 \times [1.20]^{\frac{40}{10}}$
 $C = 0.3500 \times 2.0736$
C = 0.72576 crore

When MM period t = 50 years from base that is 15 August 1947. What is C ?

Therefore, $C = 0.3500 \times [1.20]^{\frac{50}{10}}$
 $C = 0.3500 \times 2.48832$
C = 0.870912 crore

When MM period t = 60 years from base that is 15 August 1947. What is C ?

Therefore, $C = 0.3500 \times [1.20]^{\frac{60}{10}}$
 $C = 0.3500 \times 2.985984$
C = 1.0450944 crore

When MM period t = 70 years from base that is 15 August 1947. What is C ?

Therefore, $C = 0.3500 \times [1.20]^{\frac{70}{10}}$
 $C = 0.3500 \times 3.5831808$
C = 1.25411328 crore

When MM period t = 80 years from base that is 15 August 1947. What is C ?

Therefore, $C = 0.3500 \times [1.20]^{\frac{80}{10}}$
 $C = 0.3500 \times 4.29981696$
C = 1.50493594 crore

When MM period t = 90 years from base that is 15 August 1947. What is C ?

Therefore, $C = 0.3500 \times [1.20]^{\frac{90}{10}}$
 $C = 0.3500 \times 5.15978035$
C = 1.80592312 crore

When MM period t = 100 years from base that is 15 August 1947. What is C ?

Therefore, $C = 0.3500 \times [1.20]^{\frac{100}{10}}$
 $C = 0.3500 \times 6.19173642$
C = 2.16710775 crore

Case-III: when, we take **K=0.40** and **MM period t = 10 years**, **C (t) = 0.4900 crore** then

from (i), Therefore, $C = 0.3500 \times \left[\frac{0.4900}{0.3500} \right]^{\frac{t}{10}}$ ----- (iii)

When MM period t = 10 years from base that is 15 August 1947. What is C ?

Therefore, $C = 0.3500 \times [1.40]^{\frac{10}{10}}$
 $C = 0.3500 \times 1.40$
C = 0.4900 crore

When MM period t = 20 years from base that is 15 August 1947. What is C ?

Therefore, $C = 0.3500 \times [1.40]^{\frac{20}{10}}$
 $C = 0.3500 \times 1.96$
C = 0.6860 crore

When MM period t = 30 years from base that is 15 August 1947. What is C ?

Therefore, $C = 0.3500 \times [1.40]^{\frac{30}{10}}$
 $C = 0.3500 \times 2.744$
C = 0.9604 crore

When MM period t = 40 years from base that is 15 August 1947. What is C ?

Therefore, $C = 0.3500 \times [1.40]^{\frac{40}{10}}$
 $C = 0.3500 \times 3.8416$
C = 1.34456 crore

When MM period t = 50 years from base that is 15 August 1947. What is C ?

Therefore, $C = 0.3500 \times [1.40]^{\frac{50}{10}}$
 $C = 0.3500 \times 5.37824$
C = 1.882384 crore

When MM period $t = 60$ years from base that is 15 August 1947. What is C ?

Therefore, $C = 0.3500 \times [1.40]^{\frac{60}{10}}$
 $C = 0.3500 \times 7.529536$
 $C = 2.6353376$ crore

When MM period $t = 70$ years from base that is 15 August 1947. What is C ?

Therefore, $C = 0.3500 \times [1.40]^{\frac{70}{10}}$
 $C = 0.3500 \times 10.5413504$
 $C = 3.68947264$ crore

When MM period $t = 80$ years from base that is 15 August 1947. What is C ?

Therefore, $C = 0.3500 \times [1.40]^{\frac{80}{10}}$
 $C = 0.3500 \times 14.7578906$
 $C = 5.16526171$ crore

When MM period $t = 90$ years from base that is 15 August 1947. What is C ?

Therefore, $C = 0.3500 \times [1.40]^{\frac{90}{10}}$
 $C = 0.3500 \times 20.6610468$
 $C = 7.23136638$ crore

When MM period $t = 100$ years from base that is 15 August 1947. What is C ?

Therefore, $C = 0.3500 \times [1.40]^{\frac{100}{10}}$
 $C = 0.3500 \times 28.9254655$
 $C = 10.1239129$ crore

Case-IV: when, we take **$K=0.60$** and **MM period $t = 10$ years**, **$C(t) = 0.5600$ crore** then

from (i), Therefore, **$C = 0.3500 \times \left[\frac{0.5600}{0.3500}\right]^{\frac{t}{10}}$** ----- (iv)

When MM period $t = 10$ years from base that is 15 August 1947. What is C ?

Therefore, $C = 0.3500 \times [1.60]^{\frac{10}{10}}$
 $C = 0.3500 \times 1.60$
 $C = 0.5600$ crore

When MM period $t = 20$ years from base that is 15 August 1947. What is C ?

Therefore, $C = 0.3500 \times [1.60]^{\frac{20}{10}}$
 $C = 0.3500 \times 2.56$
 $C = 0.8960$ crore

When MM period $t = 30$ years from base that is 15 August 1947. What is C ?

Therefore, $C = 0.3500 \times [1.60]^{\frac{30}{10}}$
 $C = 0.3500 \times 4.096$
 $C = 1.4336$ crore

When MM period $t = 40$ years from base that is 15 August 1947. What is C ?

Therefore, $C = 0.3500 \times [1.60]^{\frac{40}{10}}$
 $C = 0.3500 \times 6.5536$
 $C = 2.29376$ crore

When MM period $t = 50$ years from base that is 15 August 1947. What is C ?

Therefore, $C = 0.3500 \times [1.60]^{\frac{50}{10}}$
 $C = 0.3500 \times 10.48576$
 $C = 3.670016$ crore

When MM period $t = 60$ years from base that is 15 August 1947. What is C ?

Therefore, $C = 0.3500 \times [1.60]^{\frac{60}{10}}$
 $C = 0.3500 \times 16.777216$
 $C = 5.8720256$ crore

When MM period $t = 70$ years from base that is 15 August 1947. What is C ?

Therefore, $C = 0.3500 \times [1.60]^{\frac{70}{10}}$
 $C = 0.3500 \times 26.8435456$
 $C = 9.39524096$ crore

When MM period $t = 80$ years from base that is 15 August 1947. What is C ?

Therefore, $C = 0.3500 \times [1.60]^{\frac{80}{10}}$
 $C = 0.3500 \times 42.949673$

C = 15.0323856 crore

When MM period t = 90 years from base that is 15 August 1947. What is C ?

Therefore, $C = 0.3500 \times [1.60]^{\frac{90}{10}}$
 $C = 0.3500 \times 68.7194768$

C = 24.0518169 crore

When MM period t = 100 years from base that is 15 August 1947. What is C ?

Therefore, $C = 0.3500 \times [1.60]^{\frac{100}{10}}$
 $C = 0.3500 \times 109.951163$

C = 38.4829071 crore

Case-V: when, we take **K=0.80** and **MM period t = 10** years, **C (t) = 0.6300** crore then

from (i), Therefore, $C = 0.3500 \times \left[\frac{0.6300}{0.3500}\right]^{\frac{t}{10}}$ ----- (v)

When MM period t = 10 years from base that is 15 August 1947. What is C ?

Therefore, $C = 0.3500 \times [1.80]^{\frac{10}{10}}$
 $C = 0.3500 \times 1.80$

C = 0.6300 crore

When MM period t = 20 years from base that is 15 August 1947. What is C ?

Therefore, $C = 0.3500 \times [1.80]^{\frac{20}{10}}$
 $C = 0.3500 \times 3.24$

C = 1.1340 crore

When MM period t = 30 years from base that is 15 August 1947. What is C ?

Therefore, $C = 0.3500 \times [1.80]^{\frac{30}{10}}$
 $C = 0.3500 \times 5.832$

C = 2.0412 crore

When MM period t = 40 years from base that is 15 August 1947. What is C ?

Therefore, $C = 0.3500 \times [1.80]^{\frac{40}{10}}$
 $C = 0.3500 \times 10.4976$

C = 3.67416 crore

When MM period t = 50 years from base that is 15 August 1947. What is C ?

Therefore, $C = 0.3500 \times [1.80]^{\frac{50}{10}}$
 $C = 0.3500 \times 18.89568$

C = 6.613488 crore

When MM period t = 60 years from base that is 15 August 1947. What is C ?

Therefore, $C = 0.3500 \times [1.80]^{\frac{60}{10}}$
 $C = 0.3500 \times 34.012224$

C = 11.9042784 crore

When MM period t = 70 years from base that is 15 August 1947. What is C ?

Therefore, $C = 0.3500 \times [1.80]^{\frac{70}{10}}$
 $C = 0.3500 \times 61.2220032$

C = 21.4277011 crore

When MM period t = 80 years from base that is 15 August 1947. What is C ?

Therefore, $C = 0.3500 \times [1.80]^{\frac{80}{10}}$
 $C = 0.3500 \times 110.199606$

C = 38.5698621 crore

When MM period t = 90 years from base that is 15 August 1947. What is C ?

Therefore, $C = 0.3500 \times [1.80]^{\frac{90}{10}}$
 $C = 0.3500 \times 198.359291$

C = 69.4257519 crore

When MM period t = 100 years from base that is 15 August 1947. What is C ?

Therefore, $C = 0.3500 \times [1.80]^{\frac{100}{10}}$
 $C = 0.3500 \times 357.046724$

C = 124.966353 crore

Case-VI: when, we take **K=0.9988** and **MM period t = 10** years, **C (t) = 0.69958** crore then

from (i), Therefore, $C = 0.3500 \times \left[\frac{0.69958}{0.3500}\right]^{\frac{t}{10}}$ ----- (vi)

When MM period $t = 10$ years from base that is 15 August 1947. What is C ?

$$\begin{aligned}\text{Therefore, } C &= 0.3500 \times [1.9988]^{\frac{10}{10}} \\ C &= 0.3500 \times 1.9988 \\ C &= \mathbf{0.69958 \text{ crore}}\end{aligned}$$

When MM period $t = 20$ years from base that is 15 August 1947. What is C ?

$$\begin{aligned}\text{Therefore, } C &= 0.3500 \times [1.9988]^{\frac{20}{10}} \\ C &= 0.3500 \times 3.99520144 \\ C &= \mathbf{1.3983205 \text{ crore}}\end{aligned}$$

When MM period $t = 30$ years from base that is 15 August 1947. What is C ?

$$\begin{aligned}\text{Therefore, } C &= 0.3500 \times [1.9988]^{\frac{30}{10}} \\ C &= 0.3500 \times 7.98560864 \\ C &= \mathbf{2.79496302 \text{ crore}}\end{aligned}$$

When MM period $t = 40$ years from base that is 15 August 1947. What is C ?

$$\begin{aligned}\text{Therefore, } C &= 0.3500 \times [1.9988]^{\frac{40}{10}} \\ C &= 0.3500 \times 15.9616345 \\ C &= \mathbf{5.58657208 \text{ crore}}\end{aligned}$$

When MM period $t = 50$ years from base that is 15 August 1947. What is C ?

$$\begin{aligned}\text{Therefore, } C &= 0.3500 \times [1.9988]^{\frac{50}{10}} \\ C &= 0.3500 \times 31.904115 \\ C &= \mathbf{11.1664403 \text{ crore}}\end{aligned}$$

When MM period $t = 60$ years from base that is 15 August 1947. What is C ?

$$\begin{aligned}\text{Therefore, } C &= 0.3500 \times [1.9988]^{\frac{60}{10}} \\ C &= 0.3500 \times 63.7699451 \\ C &= \mathbf{22.3194808 \text{ crore}}\end{aligned}$$

When MM period $t = 70$ years from base that is 15 August 1947. What is C ?

$$\begin{aligned}\text{Therefore, } C &= 0.3500 \times [1.9988]^{\frac{70}{10}} \\ C &= 0.3500 \times 127.463366 \\ C &= \mathbf{44.6121781 \text{ crore}}\end{aligned}$$

When MM period $t = 80$ years from base that is 15 August 1947. What is C ?

$$\begin{aligned}\text{Therefore, } C &= 0.3500 \times [1.9988]^{\frac{80}{10}} \\ C &= 0.3500 \times 254.773776 \\ C &= \mathbf{89.1708216 \text{ crore}}\end{aligned}$$

When MM period $t = 90$ years from base that is 15 August 1947. What is C ?

$$\begin{aligned}\text{Therefore, } C &= 0.3500 \times [1.9988]^{\frac{90}{10}} \\ C &= 0.3500 \times 509.241823 \\ C &= \mathbf{178.234638 \text{ crore}}\end{aligned}$$

When MM period $t = 100$ years from base that is 15 August 1947. What is C ?

$$\begin{aligned}\text{Therefore, } C &= 0.3500 \times [1.9988]^{\frac{100}{10}} \\ C &= 0.3500 \times 1017.87256 \\ C &= \mathbf{356.255396 \text{ crore}}\end{aligned}$$

IV. MATHEMATICAL RESULTS-IV

From case-I, case-II, case-III, case-IV, case-V and case-VI, we can write the above mathematical results in tabular form of the following:

Table-I

MM period 't' years	MEV constant 'K' 0.20	0.40	0.60	0.80	0.9988	Mean-IV $\sum C_i / N$ (crore)
10	0.4200	0.4900	0.5600	0.6300	0.69958	0.559916
20	0.5040	0.6860	0.8960	1.1340	1.3983205	0.9236641
30	0.6048	0.9604	1.4336	2.0412	2.79496302	1.5669926
40	0.72576	1.34456	2.29376	3.67416	5.58657208	2.72496242
50	0.870912	1.882384	3.670016	6.613488	11.1664403	4.84064806
60	1.0450944	2.6353376	5.8720256	11.9042784	22.3194808	8.75524336
70	1.25411328	3.68947264	9.39524096	21.4277011	44.6121781	16.0757412
80	1.50493594	5.16526171	15.0323856	38.5698621	89.1708216	29.8886536
90	1.80592312	7.23136638	24.0518169	69.4257519	178.234638	56.1498992
100	2.16710775	10.1239129	38.4829071	124.966353	356.255396	106.399135
$\sum C_i / N$ (crore)	1.09026495	3.42086952	10.1687752	28.0386794	71.223839	22.7884855

Table- II: STATISTICAL STUDY OF CORRUPTION FOR PART-IV

Data x	Frequency f	f. x	D= (x- X)	D ²	f. D ²
10	0.559916	5.59916	-78	6084	3406.52894
20	0.9236641	18.473282	-68	4642	4287.64875
30	1.5669926	47.009778	-58	3364	5271.36311
40	2.72496242	108.998497	-48	2304	6278.31342
50	4.84064806	242.032403	-38	1444	6989.8958
60	8.75524336	525.314602	-28	784	6864.11079
70	16.0757412	1125.30188	-18	324	5208.54015
80	29.8886536	2391.09229	-8	64	1912.87383
90	56.1498992	5053.49093	2	4	224.599597
100	106.399135	10639.9135	12	144	15321.4754
	N= $\sum f$ =227.88	$\sum f. x$ =20157.2264			$\sum f. D^2$ = 55765.3497

$$X = \text{Mean} = \frac{\sum f.x}{N} = \frac{20157.2264}{227.88} = 88.4554432 \approx 88$$

Therefore, **Mean =88**

We know that the formula for Standard Deviation is as follows:

$$\text{Therefore, S. D.} = \sigma = \sqrt{\frac{\sum f D^2}{N}} = \sqrt{\frac{55765.3497}{227.88}} = \sqrt{244.713664}$$

$$\text{S. D.} = \sigma = \mathbf{15.6433265}$$

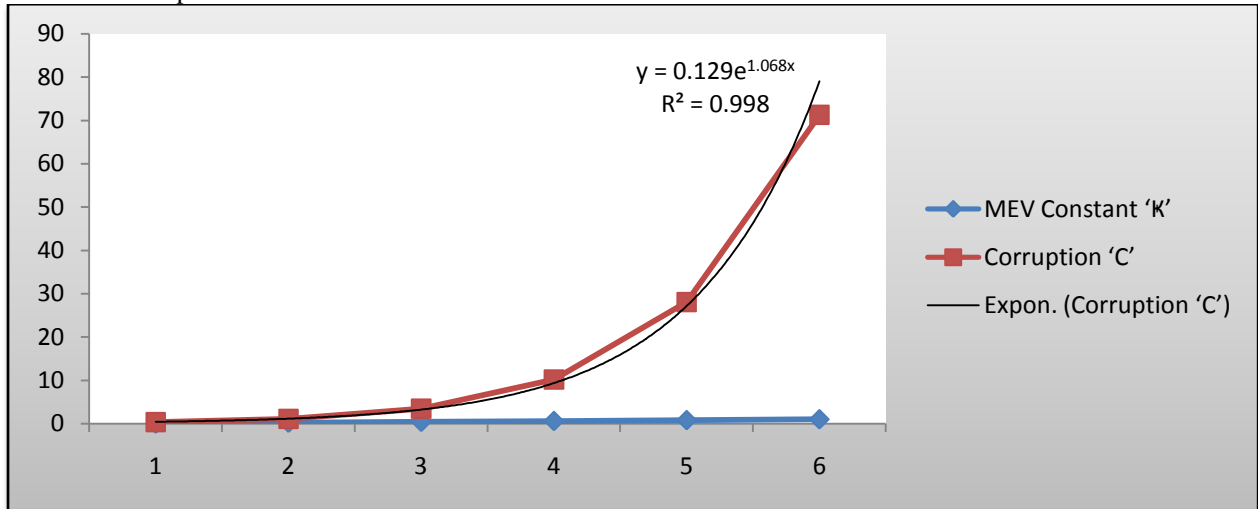
Therefore the standard deviation of corruption in India with related period is 15.6433265.

STATISTICAL GRAPH OF PART-IV:

MEV Constant 'K'	Corruption 'C'
0	0.3500
0.20	1.09026495
0.40	3.42086952
0.60	10.1687752

0.80	28.0386794
0.9988	71.223839

Graph-I: THE GRAPH BETWEEN MEV CONSTANT 'K' AND CORRUPTION 'C'



V. CONCLUSION:

We have observed that when we assumed value 1%, $C(0) = C_0 = 0.3500$ crore. The Results are distributed in population size as

- **First stage corruption:**
When $0 < K \leq 0.40$, $C = 3.42086952$ crore.
- **Medium stage corruption:**
When $0.40 < K \leq 0.80$, $C = 24.6178099$ crore.
- **Final stage corruption:**
When $0.80 < K < 1$, $C = 43.1851596$ crore.

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