Back-to-Back PWM Converter Fed PMSG Wind Turbine System

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Abstract: This paper presents a DC-link voltage controller using feedback linearization technique for the PMSG wind power system for the grid voltage sag. The DC-link voltage control is achieved by the generator side converter instead of the grid-side converter. Considering the nonlinear relationship between the generator speed ($\omega_m$) and DC-link voltage ($v_{dc}$), a DC-link voltage controller using feedback linearization technique is verified with PI and FUZZY controllers. The grid-side converter controls the grid power for MPPT. The validity of this control algorithm has been verified by simulation results for 2MW PMSG wind power system.

Keywords: Back-to-Back PWM converter, feedback linearization, MPPT, wind power system.

I. INTRODUCTION

Wind power generation is the most rapidly growing energy source. Direct-drive wind energy conversion systems based on PMSG (Permanent-Magnet Synchronous Generator) have some advantages such as no gearbox, high power density, high precision, and simple control method [1], [2]. In order to achieve objectives such as continuity and security, high levels of wind power are confronted with new challenges as well as other new approaches in the power system operation. Therefore some countries have issued dedicated grid codes for connecting the wind power systems to the grid [3]. Lately, the micro- and smart-grid have been researched for the efficiency of power management [4]. However, in these systems, the grid voltage is much fluctuated in comparison with the conventional grid. Therefore, robust control of the wind power generation system is needed for grid variations. A typical configuration of a PMSG wind power system is illustrated in Fig. 1. The synchronous generator is connected to the grid through a full-scale back-to-back converter. This converter is composed of the generator side converter and the grid-side converter.

In general, DC-link voltage is controlled by the grid side converter. The grid-side converter may be out of control for the grid voltage sags in the conventional control method. When the grid fault happens, the DC-link voltage is increased due to the continuous operation of wind turbine and generator. In the proposed method, the generator-side converter controls the DC-link voltage, and the grid-side converter controls the power of the PMSG wind turbine system. The DC-link voltage control strategy by the generator-side converter has been proposed in [5], [6], [7]. In the papers [5], [6], the DC link voltage controller is not regarded as the nonlinear characteristic of wind power system. In this paper, the DC-link voltage controller using feedback linearization technique is verified with PI and FUZZY controllers. The validity of the control algorithm has been verified by simulation results for 2MW PMSG wind power system.

II. PMSG WIND POWER SYSTEM

Wind Turbine System

The mechanical power of wind turbine is formulated as:

$$\dot{\nu} = \frac{1}{2} \rho A C_p \nu_r (\lambda, \beta) \nu_m$$ \hspace{1cm} (1)

Where $\dot{\nu}$: turbine power [W],
$\rho$: air density [kg/m$^3$],
$A$: swept area [m$^2$],
$C_p$: power conversion coefficient,
\( V_{wind} \): wind speed [m/s].

The power conversion coefficient is a function of TSR (Tip-Speed Ratio, \( \lambda \)) and pitch angle(\( \beta \)), in which TSR is defined as:

\[
TSR(\lambda) = \frac{R \omega}{V_{wind}}
\]  

(2)

The wind turbine is normally characterized by \( Pt - \omega m \) and \( Cp - \lambda \) curve as illustrated in Fig. 2. The turbine power is determined by the power conversion coefficient and TSR if the swept area, air density, and wind speed are constant. The power conversion coefficient and TSR depend on the aerodynamic characteristics of wind turbine. From Fig. 2, the maximum turbine power is found at point \( \lambda_{opt} \) and \( C_{pmax} \).

![Fig. 2. Wind turbine characteristic.](image)

(a) \( Pt - \omega m \) curve, (b) \( Cp - \lambda \) curve

![Fig. 3. Power flow of the PMSG wind power system](image)

**Modeling of PMSG**

In the synchronous d-q coordinates, the voltage equation of the PMSG is expressed as follows:

\[
V_{ds} = R_{s} i_{ds} + L_{d} \frac{di_{ds}}{dt} - \omega_{r} L_{q} i_{qs}
\]

(3)

\[
V_{qs} = R_{s} i_{qs} + L_{q} \frac{di_{qs}}{dt} + \omega_{r} L_{d} i_{ds} + \omega_{r} \lambda_{f}
\]

(4)

Where \( i_{ds}, i_{qs} \): d-q axis stator currents, \( R_{s}, L_{s} \): stator resistance and inductance, \( L_{d}, L_{q} \): d-q axis inductance, \( \Omega_{r} \): electrical angular velocity, \( \Lambda_{f} \): magnet flux.

In the generator equipped with surface-mounted permanent magnets, d- and q-axis inductance are same \( (L_{d} = L_{q}) \). The electromagnetic torque \( T_{e} \) is represented as:

\[
T_{e} = \frac{3}{2} P \frac{\lambda_{f}}{2} i_{qs}
\]

(5)

**III. GENERATOR-SIDE CONVERTER CONTROL**

The operation of the grid-side converter is directly affected by grid voltage drop and then the power transferred to the grid is decreased. However, the wind turbine and generator still operate as if it is in normal condition. Therefore, in the DC-link, excessive power transferred from the generator side makes the DC-link voltage increase. To design the DC-link voltage controller, the dynamic characteristic of the whole system is considered. Neglecting the converter loss in Fig. 3, the generator power and the DC-link capacitor power can be written as:

\[
P_{g} = P_{g} - P_{j} - P_{g,loss}
\]

(6)

\[
P_{cap} = \frac{\frac{dV_{dc}}{dt}}{G_{dc}} = P_{g} - P_{grid}
\]

(7)

Where \( PJ \): inertia power

\( P_{g, loss} \): generator loss
Combining (6) and (7), a dynamic equation for the PMSG wind turbine system can be expressed as:

\[
\begin{align*}
C_v \frac{dV_d}{dt} &= -\frac{1}{2} P_d (\frac{R}{\lambda}) \omega_\alpha - J_c \frac{d\omega}{dt} \\
&\quad - P_{iuv} - P_{pwl}
\end{align*}
\]

(8)

In this work, the nonlinear equation in (8) will be linearized using the feedback linearization technique, which is described in the next section. The power flow of the whole system is shown in Fig. 3.

**DC-link Voltage Control Adapting to Feedback Linearization**

A SISO (single input and single output) nonlinear system can be expressed as follows [8]:

\[
\begin{align*}
\begin{bmatrix} x_1 \\ x_2 \end{bmatrix} &= \begin{bmatrix} f_1(x) \\ f_2(x) \end{bmatrix} + \begin{bmatrix} g_1(x) \\ g_2(x) \end{bmatrix} u \\
y &= h(x)
\end{align*}
\]

(9)

(10)

where \( x \) : state vector, \\
u : control inputs, \\
y : outputs, \\
f, g : smooth vector fields, \\
h : smooth scalar function.

Comparing (6) and (7)-(10), we get

\[
\begin{align*}
 x_1 &= V_{dc} \\
 x_2 &= \omega_m \\
f_1(x) &= -\frac{1}{C_v} P_{grid} \\
f_2(x) &= -\frac{1}{J_c} J_\alpha - P_{iuv}
\end{align*}
\]

\[
g_1(x) = -\frac{1}{C_v} \omega_m \\
g_2(x) = -\frac{1}{J_c} \omega_m
\]

\( u = P_g \)

Here, the DC-link voltage \( v_{dc} \) is selected as the output. Next, the output of the system is differentiated as

\[
y' = A(x) + E(x) \cdot u
\]

(11)

where \( A(x) = \frac{1}{C_v} P_{grid} \), \( E(x) = \frac{1}{C_v} \)

If control input \( u \) is chosen as

\[
u = E^{-1}(x) \left[ -A(x) + y \right]
\]

(12)

where \( v \) is the equivalent control input to be specified, the resulting dynamics become linear as

\[
y' = v
\]

(13)

Note that the idea of feedback linearization, i.e., of decoupling the nonlinearities and imposing a desired linear dynamics, can be simply applied to a class of nonlinear systems.

To eliminate tracking error in the presence of parameter variations, the new control input with integral control is given by

\[
y = y_{ref} - k_1 e - k_2 \int e \, dt
\]

(14)

Where \( e = y - y_{ref} \), \\
yref : tracking reference \\
k1, k2 : controller gains.
The gains can be determined by pole placement technique. The nonlinear DC-link voltage control block diagram is shown in Fig. 4.

From the power balance condition at the DC-link, the generator power reference is selected to be the same as the grid power. The control block diagram of the generator is shown in Fig. 5.

IV. GRID-SIDE CONVERTER CONTROL

The maximum power of the wind turbine is calculated as maximum power coefficient and optimal tip-speed ratio.

\[
P_{m} = \frac{1}{2} \rho A C_{p,\text{opt}} \left( \frac{R_{\infty}}{\lambda_{\text{opt}}} \right)^{3} = K_{\text{opt}} \cdot a_{m} \tag{15}
\]

where \( K_{\text{opt}} = \frac{1}{2} \rho A C_{p,\text{opt}} \left( \frac{R}{\lambda_{\text{opt}}} \right)^{3} \)

From (8) and (15), the grid power reference is given by:

\[
P_{g} = K_{\text{opt}} \cdot a_{m}^{3} - J_{\omega} \frac{d\omega}{dt} - P_{\text{loss}} - C_{v} \frac{dv_{g}}{dt} \tag{16}
\]

The control block diagram of the grid-side converter is shown in Fig. 6.

V. SIMULATION RESULTS

The performance assessment of the DC-link voltage controller using feedback linearization technique with PI and FUZZY controllers for Back-to-Back PWM converter fed PMSG wind turbine system is verified using MATLAB.
The simulation diagram and wave forms of Back-to-Back PWM converter fed PMSG wind turbine system are shown below.

![Simulation Diagram](image1)

Fig. 7. MATLAB Simulation Diagram of Back-to-Back PWM converter fed PMSG wind turbine system.

The simulation results have shown performances of the DC-link voltage control for 50% drop of the grid voltage for 1 second. The DC-link voltage has been controlled within less than 6%. Fuzzy controller provides good dynamic response than PI controller. The simulation diagram and waveforms of PI controller are shown in Fig. 8.

![Waveforms](image2)

**a). With grid disturbance Pi Controller**

**b). Wind Speed**

**c). DC Capacitor Voltage**

**d). Generator Power**
The simulation diagram and wave forms of fuzzy controllers are shown in Fig9.

**Fig.8. Simulation waveforms of Back-to-Back PWM converter fed PMSG wind turbine system with PI Controller.**

**Fig.9. Simulation waveforms of Back-to-Back PWM converter fed PMSG wind turbine system with Fuzzy Logic Controller.**

VI. CONCLUSION

This paper presents the performance assessment of a DC-link voltage controller using feedback linearization technique with PI and FUZZY controllers for the variable speed wind turbine with PMSG for the grid voltage.
sags. This method is based on the DC-link voltage control by the generator-side converter. The grid-side converter controls the grid power according to MPPT strategy. The validity of the control algorithm has been verified by simulation results for 2MW PMSG wind power system. The simulation results have shown performances of the DC-link voltage control for 50% drop of the grid voltage for 1 second. The DC-link voltage has been controlled within less than 6%. Fuzzy controller provides good dynamic response than PI controller.

REFERENCES


