

## Design Analysis of 5 Tonne Hydraulic Jack

Aminu Saleh Mohammed<sup>1</sup>, Abdulmalik O. Ibrahim<sup>2</sup>, I. Garba<sup>3</sup>

<sup>1,2</sup>(Hydraulic Equipment Development Institute, Kumbotso.P.M.B 3067 Kano, Nigeria)

<sup>3</sup>(Department of Mechanical Engineering, Bayero University Kano, Nigeria)

Corresponding Author: Aminu Saleh Mohammed

**Abstract:** This paper present detailed parts design analysis for production of 5 tonne hydraulic jack. The study focuses its attention on the design of the hydraulic jack parts that are involved in production of the jack. Such as piston, cylinder, jack base etc. the main objective of the study is to come-up with production line of the equipment with locally available materials that could be used as a milestone for mass production of the jack.

**Keywords:** Hydraulic machines, Hydraulic jack, Piston, Cylinder

Date of Submission: 11-05-2018

Date of acceptance: 28-05-2018

### I. INTRODUCTION

Hydraulic machineries are machines and tools which use fluid power to do work. In this type of machine, high pressure liquid called hydraulic fluid is transmitted throughout the machine to various channels where it will be converted to work that will overcome a load. The fluid is controlled directly or automatically by control valves and distributed through hoses or tubes.

The popularity of hydraulic machineries is due to the very large amount of power that can be transferred through small tubes, and the high power density and wide array of actuators that can make use of this power. In hydraulics, the powering medium is liquid while gas is the powering medium for pneumatics. A very good example of this equipment is a hydraulic jack.

### II. MATERIAL AND METHODS

Hydraulic jack is a fluid processed device which is used to lift heavy load(s) by the application of much smaller force. This device works on the principle of "Pascal law of pressure" which states that "intensity of pressure is transmitted equally in all directions through a mass of fluid at rest [5].

The working mechanism of a hydraulic jack may be explained with the help of diagram below:

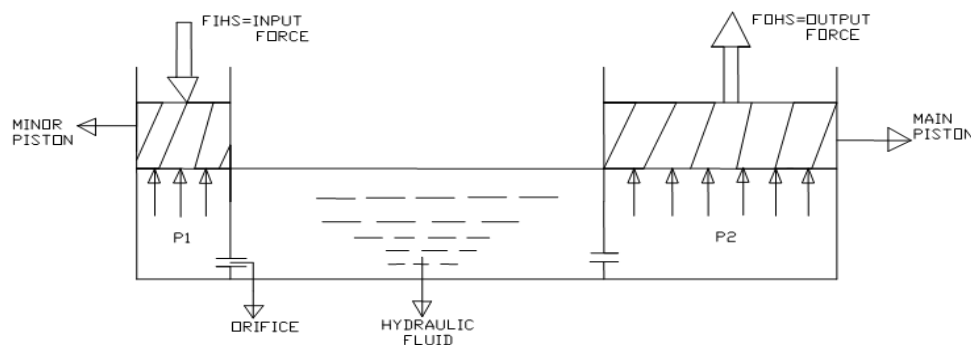


Fig 1.0: Schematic Diagram of Hydraulic jack

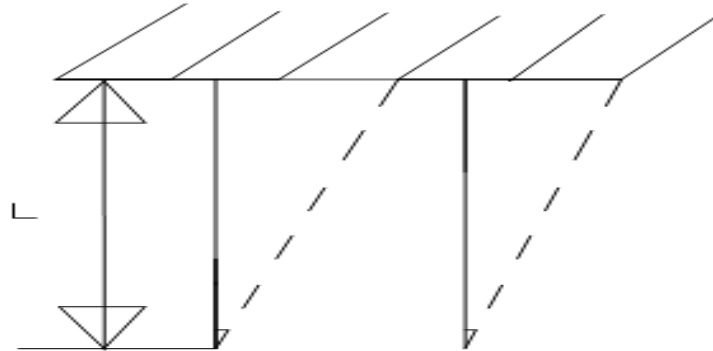
In the diagram above, the system comprises of a main piston and minor piston operating in two cylinders of different diameters that are inter-connected at the base, through a chamber which is filled with incompressible fluid. As force is supplied externally, on the minor piston, pressure  $P_1$  is exerted at the minor cylinder. Based on the principle of Pascal's law of pressure, the pressure  $P_1$  is transmitted through the channel to the main cylinder which has a bigger cross sectional area. Here, the pressure  $P_2$  is exerted on the bigger piston to produce the work which could be used to overcome the load.

It should be noted that high pressure is generated and care must be taken to prevent pressure loss which might adversely affect the efficiency of the machine [10].

**2.1DESIGN ANALYSIS(MAIN PISTON)**

**2.1.0 DESIGN CRITERIA**

1. The element is taken as a column because of the operating condition.
2. To reduce failure due to buckling and ensure convenience lift to carry out minor repair or maintenance on the part of automobile, a lift of distance 100mm is selected.
3. Base on the operating condition, steel AISI1020 Hot rolled with  $\sigma_y = 207 \text{ Mpa}$  is selected.
4. By virtue of the operating condition, “fixed – free” fixity ends with stress factor  $k = 2$  are selected.



**Fig 4.0:** A fixed – free ends column

**2.1.1 TO DETERMINE TYPE OF COLUMN,**

$$D = \left\{ \frac{64nP(KL)^2}{\pi^3 E} \right\}^{1/4} \dots\dots\dots(\text{VII})$$

Where: D = Column diameter (mm)  
 n = Design factor  
 P = Load (49050N is given)  
 K = Stress factor  
 L = Distance of lift  
 (100mm is selected to ensure safety of the operator)  
 E = Modulus of elasticity for steel is 207 GPa

Let  $n = 4$  (shock and impact energy is required on the column)

$$D = \left\{ \frac{64 \times 4 \times 49050 \times (2 \times 0.1)^2}{\pi^3 \times 207 \times 10^9} \right\}^{1/4}$$

$$D = 0.0167\text{m}$$

$$\approx 16.7\text{mm}$$

$$r = \frac{D}{4} \dots\dots\dots(\text{VIII})$$

where: r = Radius of gyration (mm)

$$r = \frac{0.0167}{4}$$

$$= 0.00418\text{m}$$

$$\text{S.R.} = \frac{KL}{r} \dots\dots\dots(\text{IX})$$

where : S.R. is Slenderness Ratio

$$\text{S.R.} = \frac{2 \times 0.1}{0.00418}$$

$$\text{S.R.} = 47.85$$

$$\text{T.R.} = \left\{ \frac{2\pi^2 E}{\sigma_y} \right\}^{1/2} \dots\dots\dots(\text{X})$$

where : T.R is Transition Ratio

$$\text{T.R.} = \left\{ \frac{2 \times \pi^2 \times 207 \times 10^9}{207 \times 10^6} \right\}^{1/2}$$

$$\text{T.R.} = 140.5$$

Note: Slender Ratio (S.R) is less than Transition Ratio (T.R), and then the column is short. Therefore the column is re-designed as short column using J.B. Johnson equation [13].

$$D = \left\{ \frac{4NP}{\pi\sigma_y} + \frac{4\sigma_y(KL)^2}{\pi^2 E} \right\}^{1/2} \dots\dots\dots(\text{XI})$$

$$D = \left\{ \frac{4 \times 4 \times 49050}{\pi \times 207 \times 10^6} + \frac{4 \times 207 \times 10^6}{\pi^2 \times 207 \times 10^9} \right\}^{1/2}$$

$$D = 0.03497$$

$$\approx 35\text{mm}$$

**2.1.2 MAIN PISTON LENGTH**

Consider the relation below:

$$\frac{D_1}{L_1} = \frac{D_2}{L_2} \dots\dots\dots(\text{XII})$$

Source: [2].

where:  $D_1$  and  $L_1$  = Diameter and length of minor piston (mm)  
 $D_2$  and  $L_2$  = Diameter and length of minor piston (mm)

$$\frac{10}{52} = \frac{35}{L_2}$$

.  $L_2 = 182\text{mm}$

Average length of minor piston adapted is 180mm

**2.1.3 PRESSURE EXACTED BY THE MAIN PISTON**

$$P = \frac{F_2}{A_2} \dots\dots\dots(\text{XIII})$$

Where:  $P$  = Working pressure ( $\text{N/m}^2$ )  
 $A_2$  = Area of main piston ( $\text{m}^2$ )

$F_2$  = Output load acting on the jack is 49050N (Given)

Because design factor ( $n$ ) is 4 in the design of main piston diameter, the pressure is considered as the working pressure and not maximum pressure, therefore the working pressure  $P$  is;

$$P = \frac{49050}{[\pi \times (0.035)^2 / 4]}$$

$$P = \frac{49050}{9.621 \times 10^{-4}}$$

$$P = 50.98 \times 10^6 \text{ N/m}^2$$

However, to determine the maximum pressure,

$$P_{\text{max}} = nP \dots\dots\dots(\text{XIV})$$

$n = 4$  was earlier selected

Where:  $P_{\text{max}}$  = Maximum pressure ( $\text{N/m}^2$ )

$$P_{\text{max}} = 4 \times 50.98 \times 10^6$$

$$= 203.6 \times 10^6 \text{ N/m}^2$$

$$= 203.6 \text{ MPa}$$

**2.1.4 MAIN CYLINDER (DESIGN CRITERIA)**

1. Base on the operating condition of the element, a thin cylindrical shell is assumed.
2. Because the piston reciprocates up and down in the cylinder, only internal pressure is taken to be exerted.
3. Because the element in thin cylindrical shell, circumferential stress is adapted [8].
4. Base on operating condition, steel AISI1144 Hot rolled, with  $\sigma_T = 640 \text{ MPa}$  is selected.
- 5.

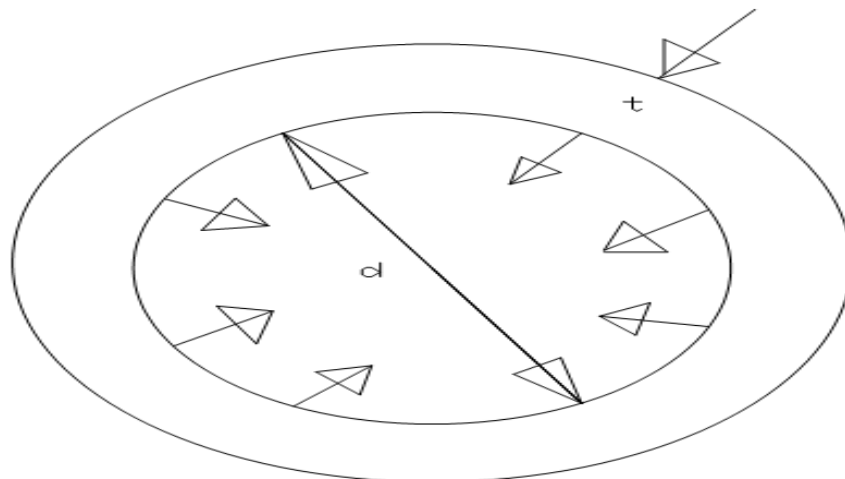


Fig 5.0: A Thin Cylindrical Shell Subjected to Internal Pressure.

$$\sigma_c = \frac{\sigma_T}{n} \dots\dots\dots (XV)$$

Where:  $\sigma_c$  = Circumferential stress (N/m<sup>2</sup>)  
 $\sigma_T$  = Tensile strength (N/m<sup>2</sup>)  
 $n$  = Design factor 3 (material and load ascertained)

$$\sigma_c = \frac{640}{3}$$

$$\sigma_c = 213.3 \times 10^6 \text{ N/m}^2$$

Take internal diameter of cylinder to be diameter of the piston + clearance 0.5 is recommended by [9].

$$d = 35 + 0.5$$

$$= 35.5 \text{ mm}$$

$$t = \frac{Pd}{2\sigma_c} \dots\dots\dots (XVI)$$

Source: (Khurmi, 2006)

Where:  $t$  = Thickness of the wall of thin cylindrical shell (m)  
 $P$  = Intensity of internal pressure  
 $= 50.9 \times 10^6 \text{ N/m}^2$  i.e. working pressure calculated.

$$t = \frac{50.98 \times 10^6 \times 0.035}{2 \times 213.3 \times 10^6}$$

$$t = 0.0042 \text{ m}$$

$$= 4.2 \text{ mm}$$

$$\approx 4 \text{ mm}$$

When the value of  $\frac{t}{d}$  is less than  $1/10^{\text{th}}$ , then it is assumed a thin cylindrical shell [9]. Therefore,  $\frac{4}{35.5} = 0.11$   
 This value is around  $1/10^{\text{th}}$ , therefore thin cylindrical shell adapted earlier is appropriate.

1. Based on hardness and fair ductility properties required, steel AISI1050 cold drawn with  $\sigma_y = 579 \text{ mpa}$  is selected [11].

Where:  $Z$  = Section modulus rectangular cross section (N/m)  
 $b$  = Thickness of Number of threads subjected to load and constraint.

$$Z = \frac{0.003b^2}{6}$$

$$Z = 0.0005b^2 \text{ N/m}^3$$

$$\sigma_{ALL} = \frac{M}{Z} \dots\dots\dots (XXV)$$

$$193 \times 10^6 = \frac{22.992}{0.0005b^2}$$

$$b = 0.0154 \text{ m}$$

$$\text{Take } b_T = \frac{b}{N} \dots\dots\dots (XXVI)$$

Where  $b_T$  = Thickness of a thread (mm)  
 $N$  = Number of threads subjected to load and constraint.

$$b_T = \frac{0.015}{N}$$

$$\sigma_b = \frac{3Wh}{2\pi N r_i (b_T)^2} \dots\dots\dots (XXVII)$$

Where:  $\sigma_b$  = Bending stress (N/m<sup>2</sup>) acting on per thread.  
 Substitute  $b_T$  in above equation

$$\sigma_b = \frac{3WhN}{2\pi r_i (0.0154)^2}$$

Let  $\sigma_b = \sigma_{ALL}$

$$193 \times 10^6 = \frac{3 \times 49050 \times 0.003 \times N}{2 \times \pi \times 0.00899 \times 0.0154^2}$$

$$N = 5.9$$

$$\approx 6$$

If the number of threads subjected to load and constraint is 6, thickness per thread;

$$b_T = \frac{0.0154}{6}$$

$$b_T = 0.0026 \text{ mm}$$

$$= 2.6 \text{ mm}$$

$$P_d = D - \sin \theta P \dots\dots\dots (XXVIII)$$

Where  $P_d$  = Pitch diameter (mm)  
 $P$  = Pitch

$$\theta = \text{Included angle of the thread, (For a square thread } \theta = 5^\circ\text{), Source: [16].}$$

$$P_d = 23 - 6\sin 5^\circ$$

$$= 22.47 \text{ mm}$$

**2.1.5 MINOR PISTON (DESIGN CRITERIA)**

1. Consider that the material selected is having same properties with material selected for main piston.
2. Take the design factor N to be same i.e. 4.
3. Assume that there is no pressure loss

From Pascal's law of pressure

$$\frac{F_1}{A_1} = \frac{F_2}{A_2} = 50.9 \times 10^6$$

Where:  $F_1$  = Input force on hydraulic system  
 = 3750 N (determined)

$A_1$  = Area of minor piston ( $m^2$ )

$$50.9 \times 10^6 = \frac{3750}{A_1}$$

$$A_1 = 7.353 \times 10^{-5} \text{ m}^2$$

$$d_1 = \left[ \frac{4A_1}{\pi} \right]^{1/2} \dots\dots\dots \text{(XXIX)}$$

Where:  $d_1$  = Minor piston diameter (mm)

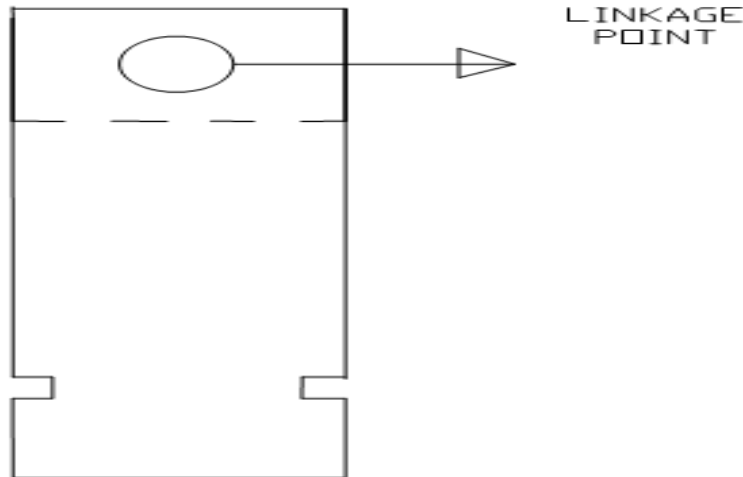
$$d_1 = \left[ \frac{4 \times 7.353 \times 10^{-5}}{\pi} \right]^{1/2}$$

$$d_1 = 9.61 \times 10^{-3} \text{ m}$$

$$d_1 = 9.6$$

$$\approx 10\text{mm}$$

**2.1.6 MINOR PISTON LENGTH**



**Fig 8.0:** Linkage Point of Minor Piston

However, note that the piston conveniently fills the cylinder at the downward stroke. The length of the piston is considered to be length of cylinder plus linkage clearance (10mm) with lever system to ensure adequate movement of the minor piston.

$$L_1 = C_L + C$$

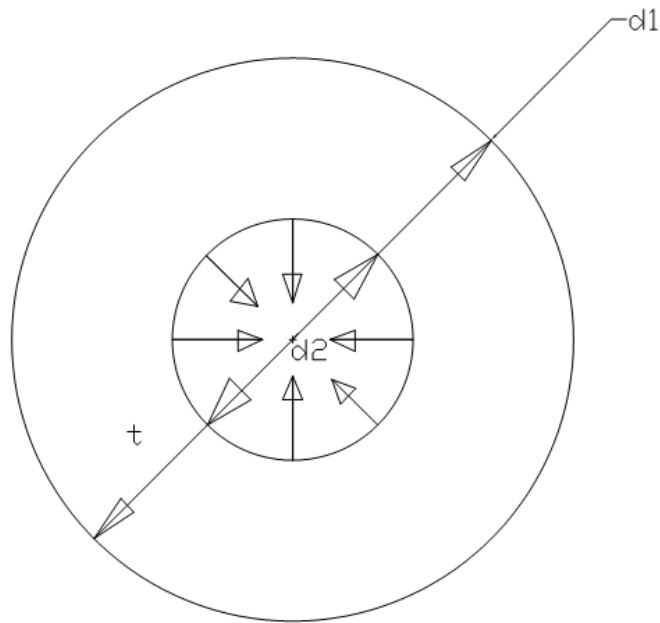
$$= 52.0 + 10$$

$$= 62.0\text{mm}$$

$$\approx 62\text{mm}$$

**2.1.8 MINOR CYLINDER (DESIGN CRITERIA)**

1. Based on the operating condition, thick wall cylindrical shell is assumed.
2. Because the piston reciprocates up and down in the cylinder, only internal pressure is considered to be exerted.
3. Based on the working condition, steel AISI1020 Hot rolled with  $\sigma_T = 392\text{mpa}$  is selected.



**Fig 9.0:** A Thick Cylindrical Shell Subjected to Internal Pressure.

Apply Lamé's equation:

$$P = \frac{b}{(r_2)^2} - a \dots\dots\dots(\text{XXX})$$

Source: [6].

Where: P = Intensity of internal pressure =  $50.9 \times 10^6 \text{ N/m}^2$   
 $r_2$  = Radius of internal wall of the cylinder (mm)  
 a and b = constants.

Take  $d_2$  = diameter of minor piston + clearance 0.5 [6].

$$= 10 + 0.5$$

$$= 10.5 \text{ mm}$$

$$r_2 = \frac{10.5}{2}$$

$$= 5.25 \text{ mm}$$

Therefore;

$$50.9 \times 10^6 = \frac{b}{(5.25 \times 10^{-3})^2} - a$$

$$a = \frac{b}{2.76 \times 10^{-5}} - 50.9 \times 10^6 \dots\dots\dots(\text{XXXI})$$

$$n = \frac{\sigma_T}{\sigma_{T(ALL)}} \dots\dots\dots(\text{XXXII})$$

Where:  $\sigma_T$  = Tensile strength =  $392 \times 10^6 \text{ N/m}^2$   
 $\sigma_{T(ALL)}$  = Allowable tensile stress ( $\text{N/m}^2$ )  
 n = Design factor is 4 (shock and impact energy required)

$$4 = \frac{392 \times 10^6}{\sigma_{T(ALL)}}$$

$$\sigma_{T(ALL)} = 98 \times 10^6 \text{ N/m}^2$$

$$\sigma_{T(ALL)} = \frac{b}{(r_2)^2} - a \dots\dots\dots(\text{XXXIII})$$

$$98 \times 10^6 = \frac{b}{2.76 \times 10^{-5}} - a$$

$$a = 98 \times 10^6 - \frac{b}{2.76 \times 10^{-5}} \dots\dots\dots(\text{XXXIV})$$

Equate equations (XXXI) and (XXXIV)

$$\frac{b}{2.76 \times 10^{-5}} - 50.9 \times 10^6 = 98 \times 10^6 - \frac{b}{2.76 \times 10^{-5}}$$

$$\frac{2b}{2.76 \times 10^{-5}} = 148.9 \times 10^6$$

$$b = 2054.82$$

Substitute b = 2054.82 in equation (XXXI)

$$a = \frac{2054.82}{2.76 \times 10^{-5}} - 50.98 \times 10^6$$

$$a = 23.47 \times 10^6$$

If only internal pressure is assumed to be exerted, external pressure is zero

$$P_2 = \frac{b}{(r_1)^2} - a \dots \dots \dots (XXXV)$$

Where:  $P_2$  = External pressure intensity = 0

$r_1$  = External radius of the cylinder (mm)

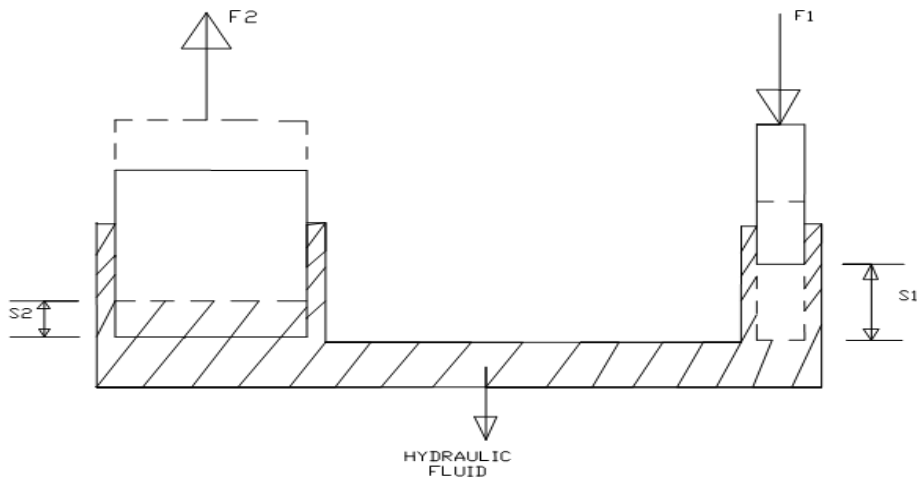
$$0 = \frac{2054.82}{r_1^2} - 23.55 \times 10^6$$

$$r_1 = 9.34 \text{ mm}$$

$$\begin{aligned} \text{Wall thickness } t &= r_1 - r_2 \\ &= 9.34 - 5.25 \\ &= 4.09 \\ &\approx 4 \text{ mm} \end{aligned}$$

Note:  $\frac{t}{d} = \frac{4}{10.5} = 0.38$

The value 0.38 is greater than  $1/10^{\text{th}}$ , therefore the thick cylindrical wall shell selected earlier is appropriate.



**Fig 10.0:** Schematic Diagram of Hydraulic Jack Operation System

- $F_1$  = Hydraulic system input force
- $F_2$  = Hydraulic system output force
- $S_1$  = Fluid displacement in minor cylinder
- $S_2$  = Fluid displacement in main cylinder

The volume of fluid displaced in the minor cylinder equals the volume of fluid that raised the main piston in the main cylinder

Source: [12].

$$V_1 = V_2$$

Take the area of minor and main pistons as the area of fluid displaced in minor cylinder and the fluid that raised the main piston respectively

$$A_1 S_1 = A_2 S_2 \dots \dots \dots (XXXVI)$$

By experiment, total number of strokes to conveniently raise the load to 100mm is averagely 50.

$$\begin{aligned} \text{Distance of lift/stroke} &= \frac{100}{50} \\ &= 2 \text{ mm} \end{aligned}$$

$$\begin{aligned} : \quad S_2 &= 2 \text{ mm} \\ 7.353 \times 10^{-5} S_1 &= 9.621 \times 10^{-4} \times 0.002 \end{aligned}$$

$$\begin{aligned} S_1 &= \text{Distance of fluid displace} = 26.17 \times 10^{-3} \text{ m} \\ S_1 &\approx 26 \text{ mm.} \end{aligned}$$

At the return stroke of the piston when the inlet is opened to release another set of fluid into the chamber, a factor 2 is selected to conveniently trap the fluid in the system thus avoid pressure loss and fluid loss. Therefore minor cylinder is taken to be twice the distance of fluid displaced.

Therefore,

$$: \quad C_L = 2S_1 \dots \dots \dots (XXXVII)$$

Where:  $C_L$  = Length of minor cylinder

$$\begin{aligned} C_L &= 2 \times 26 \\ &= 52 \text{ mm.} \end{aligned}$$

### **2.1.9 MAIN CYLINDER LENGTH**

If the main piston length is taken as 180mm and the required distance of lift of the load is 100mm (earlier recommended).

Note: at the start of the operation, the whole of the main piston is inside the main cylinder. So clearance is required.

Therefore, to allow some part of the piston to remain in the cylinder at the maximum lift distance, and also to ensure that there is no pressure or fluid loss, the main cylinder length selected is 150mm.

### **III. CONCLUSION AND FUTURE WORK**

This report has presented a detailed design analysis for production of 5 tonne hydraulic jack, the engineering drawings of all the parts were developed using two approaches namely conventional and reverse engineering.

Conventional engineering team were able to design the jack by producing the design calculations, detailed drawings and cost of producing each component involve for the development of the prototype. While reverse engineering team were able to produce the jack through reverse engineering approach, material of the jack parts were identified through spark test and some other tests.

The base of the jack was successfully produced, tested and its performance was very good. Some of the components that were locally produced includes: Main cylinder, main cylinder, minor piston and jack base etc.

Henceforth, this paper recommend on the increase in the tonnage from 5 to 20 tonne in the future and attention should also focus on elemental analysis and hardness test of each part

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Aminu Saleh Mohammed "Design Analysis Of 5 Tonne Hydraulic Jack "IOSR Journal of Engineering (IOSRJEN), vol. 08, no. 5, 2018, pp. 35-42