

Flow and Heat transfer in a MHD Viscoelastic Fluid over a Stretching Sheet with viscous dissipation and Work due to Deformation

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I. INTRODUCTION

Boundary-layer behavior over a moving continuous solid surface is an important type of flow occurring in several engineering processes. Such processes include heat-treated materials travelling between a feed roll and a wind-up roll or materials manufactured by extrusion and many others. Since the pioneering work of Sakiadis [1], various aspects of the problem have been investigated by many authors. Crane [2], Gupta and Gupta [3] have analyzed the stretching problem with constant surface temperature, while Soundalgekar [4] investigated the Stokes problem for a viscoelastic fluid. This flow was examined by Siddappa and Khapate [5] for a special class of non-Newtonian fluids known as second-order fluids, which are viscoelastic in nature. Danberg and Fansler [6] studied the solution for the boundary layer flow past a wall that is stretched with a speed proportional to the distance along the wall.

Rajagopal et al. [7] independently examined the same flow as in [5] and obtained similarity solutions of the boundary-layer equations numerically for the case of small viscoelastic parameter k_1 . It is shown that skin-friction decreases with increase in k_1 . Dandapat and Gupta [8] examined the same problem with heat transfer. In [8], an exact analytical solution of the non-linear equation governing this self-similar flow which is consistent with the numerical results in [7] is given and the solutions for the temperature for various values of k_1 are presented. Later, Cortell [9] extended the work of Dandapat and Gupta [8] to study the heat transfer in an incompressible second-order fluid caused by a stretching sheet with a view to examining the influence of the viscoelastic parameter on that flow. It is found that the temperature distribution depends on k_1 , in accordance with the results in [8].

In the case of fluids of differential type (see Ref. [10]), the equations of motion are in general one order higher than the Navier–Stokes equations and, they need additional boundary conditions to determine the solution completely. These important issues were studied in detail by Rajagopal [10], [11] and Rajagopal and Gupta [12]. On the other hand, Abel and Veena [13] investigated a viscoelastic fluid flow and heat transfer in a porous medium over a stretching sheet and observed that the dimensionless surface temperature profiles increases with an increase in viscoelastic parameter k_1 ; however, later, Abel et al. [14] studied the effect of heat transfer on MHD viscoelastic fluid over a stretching surface and an important finding was that the effect of visco-elasticity is to decrease the dimensionless surface temperature profiles in that flow. Furthermore, Char [15] studied MHD flow of a viscoelastic fluid over a stretching sheet; however, only the thermal diffusion is considered in the energy equation. Vajravelu and Rollins [16] obtained analytical solution for heat transfer characteristics in viscoelastic second order fluid over a stretching sheet with frictional heating and internal heat generation. Later, Sarma and Rao [17] extended the work of

Vajravelu and Rollins [16] and studied the effect of work due to deformation in the energy equation. Vajravelu and Roper [18] and Cortell [19] analyzed the effects of work due to deformation in viscoelastic second grade fluid over a stretching sheet. Another effect which bears great importance on heat transfer is the viscous dissipation. When the viscosity of the fluid and/or velocity gradient is high, the dissipation term becomes important. Consequently, the effects of viscous dissipation are also included in the energy equation

In the present paper, the flow and heat transfer of an incompressible MHD viscoelastic fluid past stretching sheet with viscous dissipation and work due to deformation terms in the energy equation are considered. Non linear boundary layer equations are solved using quasilinearization technique with two thermal boundary conditions, namely, (i) the sheet with Constant Surface Temperature (CST case) (ii) the sheet with Prescribed Surface Temperature (PST case). Results are in good agreement with available studies. This paper highlights the effect of work due to deformation on heat transfer characteristics of the fluid.

II. MATHEMATICAL FORMULATION

Following the postulates of gradually fading memory, Coleman and Noll [20] derived the constitutive equation of second-order fluid flow in the form

$$T = -pI + \mu A_1 + \alpha_1 A_2 + \alpha_2 A_1^2 \quad (1)$$

where T is the Cauchy stress tensor, $-pI$ is the spherical stress due to constraint of incompressibility, μ is the dynamics viscosity, α_1, α_2 are the material constants and A_1 and A_2 are the first two Rivlin–Ericken tensors [21] defined as

$$A_1 = (\text{grad } v) + (\text{grad } v)^T \quad (2)$$

$$A_2 = \frac{dA_1}{dt} + A_1(\text{grad } v) + (\text{grad } v)^T A_1 \quad (3)$$

Here, v denotes the velocity field and d/dt is the material time derivative. If the fluid of second grade modeled by (1) is to be compatible with thermodynamics and is to satisfy the Clausius-Duhem inequality for all motions and the assumption that the specific Helmholtz free energy of the fluid is a minimum when it is locally at rest, Dunn and Fosdick [22] found that the material moduli must satisfy

$$\mu \geq 0, \alpha_1 \geq 0, \alpha_1 + \alpha_2 = 0 \quad (4)$$

But later on Fosdick and Rajagopal [23] have reported, by using the data reduction from experiments, that in the case of a second order fluid the material constants μ, α_1, α_2 should satisfy the relation

$$\mu \geq 0, \alpha_1 \leq 0, \alpha_1 + \alpha_2 \neq 0 \quad (5)$$

They also reported that that the fluids modeled by (1) with the relationship (5) exhibit some anomalous behavior. A critical review on this controversial issue can be found in the work of Dunn and Rajagopal [24]. It was mentioned that second-order fluid, obeying model equation (1) with $\alpha_1 < \alpha_2, \alpha_1 < 0$ although exhibits some undesirable instability characteristics, the second order approximations are valid at low shear rate. Now in literature the fluid satisfying the model equation (1) with $\alpha_1 < 0$ is termed as second-order fluid and with $\alpha_1 > 0$ is termed as second grade fluid.

In present study, it is considered a laminar steady flow of an incompressible MHD viscoelastic (Walters' liquid B model) fluid over a wall coinciding with the plane $y = 0$, the flow being confined to $y > 0$. Two equal and opposite forces are applied along the x-axis, so that a sheet is stretched with a velocity proportional to the distance from the origin. The resulting motion of the quiescent fluid is thus caused solely by the moving surface. The flow satisfies the rheological equation of state derived by Beard and Walters [25]. The governing boundary layer equations for momentum, in the usual form, are

$$\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} = 0 \quad (6)$$

$$u \frac{\partial u}{\partial x} + v \frac{\partial v}{\partial y} = \nu \frac{\partial^2 u}{\partial y^2} - k_0 \left\{ \frac{\partial}{\partial x} \left(u \frac{\partial^2 u}{\partial y^2} \right) + \frac{\partial u}{\partial y} \frac{\partial^2 v}{\partial y^2} + v \frac{\partial^3 u}{\partial y^3} \right\} - \frac{\sigma B_0^2 u}{\rho} \quad (7)$$

$$\text{where } \nu = \frac{\mu}{\rho}, k_0 > 0$$

where u and v are the velocity components along the x and y directions respectively, ν are the kinematic viscosity, $k_0 = -\alpha_1 / \rho$ is the co-efficient of elasticity, and ρ is the density. Hence, in the case second order fluid flow k_0 takes positive value as α_1 takes negative value and other quantities have their usual meanings. In

deriving (7) it is assumed that the normal stress is of the same order of magnitude as that of the shear stress, in addition to usual boundary layer approximations.

The boundary conditions for the velocity field are:

$$\begin{aligned}
 u = u_w = bx, \quad v = 0 \quad \text{at } y = 0, b > 0 \\
 u \rightarrow 0, \quad \frac{\partial u}{\partial x} \rightarrow 0 \quad \text{as } y \rightarrow \infty
 \end{aligned}
 \tag{8}$$

The condition $\frac{\partial u}{\partial y} \rightarrow 0$ as $y \rightarrow \infty$ is the augmented condition since the flow is in an unbounded domain, which has been discussed by Rajgopal [10]. In this case, the flow is caused solely by the stretching of the sheet, since the free stream velocity is zero.

Defining new variables:

$$u = bx f_\eta(\eta), \quad v = -\sqrt{b\nu} f(\eta), \quad \eta = \sqrt{b/\nu} y
 \tag{9}$$

where $f_\eta(\eta)$ denotes differentiation with respect to η . Clearly u and v defined above satisfy the continuity equation (6), and equation (7) is transformed as

$$f_\eta^2 - ff_{\eta\eta} = f_{\eta\eta\eta} - k_1 \{ 2f_\eta f_{\eta\eta\eta} - ff_{\eta\eta\eta\eta} - f_{\eta\eta}^2 \} - Mn f_\eta
 \tag{10}$$

where $k_1 = \frac{k_0 b}{\nu}$ is the viscoelastic parameter, $Mn = \frac{\sigma B_0^2}{\rho b}$ is magnetic parameter.
 The boundary conditions (8) become

$$f(0) = 0, \quad f_\eta(0) = 1
 \tag{11a}$$

$$f_\eta(\eta) \rightarrow 0, \quad f_{\eta\eta}(\eta) \rightarrow 0 \quad \text{as } \eta \rightarrow \infty
 \tag{11b}$$

III. HEAT TRANSFER ANALYSIS

By using boundary layer approximations, and taken into account both viscous dissipation and work due to deformation, the equation of energy for temperature T is given by

$$\rho C_p \left(u \frac{\partial T}{\partial x} + v \frac{\partial T}{\partial y} \right) = k \frac{\partial^2 T}{\partial y^2} + \mu \left(\frac{\partial u}{\partial y} \right)^2 - \rho k_0 \frac{\partial u}{\partial y} \left[\frac{\partial}{\partial y} \left(u \frac{\partial u}{\partial x} + v \frac{\partial u}{\partial y} \right) \right]
 \tag{12}$$

where k is the thermal diffusivity and C_p the specific heat of a fluid at constant pressure. Two thermal boundary conditions are considered, namely, (i). Constant Surface Temperature (CST case)
 (ii). Prescribed Surface Temperature (PST case)

The heat transfer analysis for these two processes is carried out in the following sections.

3.1 Constant Surface Temperature (CST case)

In this circumstance, the boundary conditions are

$$T = T_w \text{ at } y = 0, \quad T \rightarrow T_\infty \text{ as } y \rightarrow y_\infty
 \tag{13}$$

Where T_w and T_∞ are constants.

Defining non-dimensional temperature and Prandtl number (Pr) as

$$\theta(\eta) = \frac{(T - T_\infty)}{(T_w - T_\infty)}, \quad Pr = \frac{\nu}{\alpha}
 \tag{14}$$

Using (9), equation (12) reduces to

$$\theta'' + \text{Pr } f\theta' = -\text{Pr } Ec \left[(f'')^2 - k_1 f'' (ff'' - ff''') \right] \quad (15)$$

With boundary conditions

$$\theta(0) = 1, \theta(\infty) \rightarrow 0 \quad (16)$$

Here $Ec = (b^2 x^2) / c_p (T_w - T_\infty)$ represents local Eckert number for this problem. It is worth mentioning that the x-coordinate cannot be eliminated from (15), whereby, the temperature profiles always depend on x.

3.2 Prescribed Surface Temperature (PST case)

For this circumstance, the boundary conditions are

$$T = T_w \left[= T_\infty + A \left(\frac{x}{l} \right)^2 \right] \quad \text{at } y=0 \quad (17a)$$

$$T \rightarrow T_\infty \quad \text{as } y \rightarrow \infty \quad (17b)$$

where l is the characteristic length.

Using (9), equation (12) reduces to

$$\theta'' + \text{Pr } f\theta' - 2\text{Pr } f'\theta = -\text{Pr } Ec \left[(f'')^2 - k_1 f'' (ff'' - ff''') \right] \quad (18)$$

with boundary conditions

$$\theta(0) = 1, \theta(\infty) \rightarrow 0$$

IV. NUMERICAL SOLUTION OF THE PROBLEM

The flow equation (10) coupled with energy equation (15) or (18) become set of nonlinear differential equations. A numerical method, quasilinearization technique [26], is in most cases directly applicable to computer aided solutions of non-linear two-point boundary value problems. So this method is used to solve this system.

For convenience equations (10), (15) and (18) are rearranged as

$$f^{iv} = \frac{1}{k_1 f} \left[(f')^2 - ff'' - f''' + Mn f' + 2k_1 f f''' - k_1 (f'')^2 \right] \quad (19)$$

$$\theta'' + \text{Pr } f\theta' = -\text{Pr } Ec \left[(f'')^2 - k_1 f'' (ff'' - ff''') \right] \quad (\text{CST case}) \quad (20a)$$

(OR)

$$\theta'' + \text{Pr } f\theta' - 2\text{Pr } f'\theta = -\text{Pr } Ec \left[(f'')^2 - k_1 f'' (ff'' - ff''') \right] \quad (\text{PST case}) \quad (20b)$$

In order to implement the quasilinearization method, the equations (19) and (20) are converted to a system of first order differential equations by substituting

$$(f, f', f'', f''', \theta, \theta') = (x_1, x_2, x_3, x_4, x_5, x_6)$$

Then equations (19) and (20) give

$$\begin{aligned} \frac{dx_1}{d\eta} &= x_2 \\ \frac{dx_2}{d\eta} &= x_3 \\ \frac{dx_3}{d\eta} &= x_4 \\ \frac{dx_4}{d\eta} &= \frac{1}{k_1 x_1} \{ x_2^2 - x_1 x_3 - x_4 + Mn x_2 + 2k_1 x_2 x_4 - k_1 x_3^2 \} \end{aligned} \quad (21)$$

$$\frac{dx_5}{d\eta} = x_6$$

$$\frac{dx_6}{d\eta} = -\text{Pr } x_1 x_6 - \text{Pr } Ec [x_3^2 - k_1 x_3 (x_2 x_3 - x_1 x_4)] \quad (\text{CST case})$$

(OR)

$$\frac{dx_6}{d\eta} = -\text{Pr } x_1 x_6 + 2 \text{Pr } x_2 x_5 - \text{Pr } Ec [x_3^2 - k_1 x_3 (x_2 x_3 - x_1 x_4)] \quad (\text{PST case})$$

Using Quasilinearization technique, the system (21) can be linearized as

$$\frac{dx_1^{r+1}}{d\eta} = x_2^{r+1}$$

$$\frac{dx_2^{r+1}}{d\eta} = x^{r+1}$$

$$\frac{dx_3^{r+1}}{d\eta} = x_4^{r+1}$$

$$\frac{dx_4^{r+1}}{d\eta} = \left(\frac{-1}{k_1 (x_1^r)^2} \left((x_2^r)^2 - x_4^r + Mnx_2^r + 2k_1 x_2^r x_4^r - k_1 (x_3^r)^2 \right) \right) x_1^{r+1}$$

$$+ \left(\frac{1}{k_1 x_1^r} (2x_2^r + 2k_1 x_4^r) \right) x_2^{r+1}$$

$$+ \left(\frac{1}{k_1 x_1^r} (-x_1^r - 2k_1 x_3^r) \right) x_3^{r+1}$$

$$+ \left(\frac{1}{k_1 x_1^r} (-1 + 2k_1 x_2^r) \right) x_4^{r+1} + \left(\frac{-x_4^r + Mnx_2^r}{k_1 x_1^r} \right) \quad (22)$$

$$\frac{dx_5^{r+1}}{d\eta} = x_6^{r+1}$$

$$\frac{dx_6^{r+1}}{d\eta} = (-\text{Pr } x_6^r - \text{Pr } Eck_1 x_3^r x_4^r) x_1^{r+1} + (\text{Pr } Eck_1 (x_3^r)^2) x_2^{r+1}$$

$$- Ec \text{Pr} (2x_3^r - k_1 (2x_2^r x_3^r - x_1^r x_4^r)) x_3^{r+1} - (\text{Pr } Eck_1 x_1^r x_3^r) x_4^{r+1} - \text{Pr } x_1^r x_6^{r+1}$$

$$+ (Ec \text{Pr} (x_3^r)^2 + \text{Pr } x_1^r x_6^r - 2 \text{Pr } Eck_1 x_3^r (x_2^r x_3^r - x_1^r x_4^r))$$

(OR)

$$\frac{dx_6^{r+1}}{d\eta} = (-\text{Pr } x_6^r - \text{Pr } Eck_1 x_3^r x_4^r) x_1^{r+1} + (2 \text{Pr } x_5^r + \text{Pr } Eck_1 (x_3^r)^2) x_2^{r+1}$$

$$+ (-2Ec \text{Pr } x_3^r + \text{Pr } Eck_1 (2x_2^r x_3^r - x_1^r x_4^r)) x_3^{r+1} - (\text{Pr } Eck_1 x_1^r x_3^r) x_4^{r+1} + (2 \text{Pr } x_2^r) x_5^{r+1}$$

$$+ (-\text{Pr } x_1^r) x_6^{r+1} + (Ec \text{Pr} (x_3^r)^2 + \text{Pr } x_1^r x_6^r - 2 \text{Pr } x_2^r x_5^r - 2 \text{Pr } Eck_1 x_3^r (x_2^r x_3^r - x_1^r x_4^r))$$

The above system of equations (22) is linear in x_i^{r+1} ($i = 1, 2, \dots, 6$) and general solution can be obtained by using the principle of superposition.

The boundary conditions reduce to

$$x_1^{r+1}(\eta)=0, x_2^{r+1}(\eta)=1, x_3^{r+1}(\eta)=1 \quad \text{at } \eta=0$$

$$x_2^{r+1}(\eta) \rightarrow 0, x_3^{r+1}(\eta) \rightarrow 0, x_5^{r+1}(\eta) \rightarrow 0 \quad \text{as } \eta \rightarrow \infty$$

The initial values are chosen as follows:

For the homogeneous solution:

$$\begin{aligned} x_i^{h_1}(\eta) &= [0 \ 0 \ 1 \ 0 \ 0 \ 0] \\ x_i^{h_2}(\eta) &= [0 \ 0 \ 0 \ 1 \ 0 \ 0] \end{aligned}$$

(23)

$$x_i^{h_3}(\eta) = [0 \ 0 \ 0 \ 0 \ 0 \ 1]$$

For particular solution:

$$x_i^p(\eta) = [0 \ 1 \ 0 \ 0 \ 1 \ 0]$$

(24)

The general solution of system of equations is given by

$$x_i^{r+1}(\eta) = c_1 x_i^{h_1}(\eta) + c_2 x_i^{h_2}(\eta) + c_3 x_i^{h_3}(\eta) + x_i^p(\eta)$$

(25)

where C_1, C_2, C_3 are the unknown constants and are determined by considering the boundary conditions as $\eta \rightarrow \infty$. This solution $(x_i^{r+1}, i = 1, 2, \dots, 6)$ is then compared with solution at the previous step $x_i^r, i = 1, 2, \dots, 6$ and next iteration is performed if the convergence has not been achieved or greater accuracy is desired.

V. RESULTS AND DISCUSSIONS

Here, a study is presented on flow and heat transfer of an incompressible second order fluid past a stretching sheet. The non linear differential equations of flow and heat transfer were solved by quasilinearization technique. The energy equation includes both the viscous dissipation and the work due to deformation. This later effect doesn't appear, if a viscous flow (i.e., $k_1=0$) takes place.

Case 1.Constant Surface Temperature (CST case):

In Fig1, values of dimensionless temperature $\theta(\eta)$ and temperature gradient $\theta'(\eta)$ for selected values of Prandtl number (Pr) with $k_1=0.3, Ec = 0$ are given. Since thermal boundary layer thickness decreases with increasing Prandtl number, temperature $\theta(\eta)$ at a point decreases with an increase in the Prandtl number.

In Fig2, temperature $\theta(\eta)$ and temperature gradient $\theta'(\eta)$ are drawn for various values of Eckert number (Ec). Temperature $\theta(\eta)$ increases with increase in viscous dissipation, because heat energy is stored in the fluid due to frictional heating. The values $|\theta'(0)|$ decrease with increase in viscous dissipation, which yields augment in fluid's temperature.

Case 2. Prescribed Surface Temperature (PST case)

In Fig3, Values of non-dimensional temperature $\theta(\eta)$ for various values of Prandtl number (Pr) are shown. In Fig 4, effect of viscous dissipation on temperature $\theta(\eta)$ and temperature gradient $\theta'(\eta)$ is depicted. The reasons are same as in CST case.

In Fig 5, the effect of work due to deformation term in the energy equation on temperature profiles for various values of Eckert number (Ec) is shown. It can be seen that, the presence of work due to deformation term in the energy equation reduces the temperature, which is in contrast to the case $\alpha_1 > 0$ [19] (i.e., second grade fluids). This effect is more significant for moderate and higher values of Eckert number (Ec).

Fig 6 depicts the effect of magnetic field parameter (Mn) on the horizontal velocity profile ($f_\eta(\eta)$). Horizontal velocity profile decreases with increase in Magnetic field parameter, since increase of Magnetic field parameter signifies the increase of Lorentz force, which opposes the horizontal flow in the reverse direction.

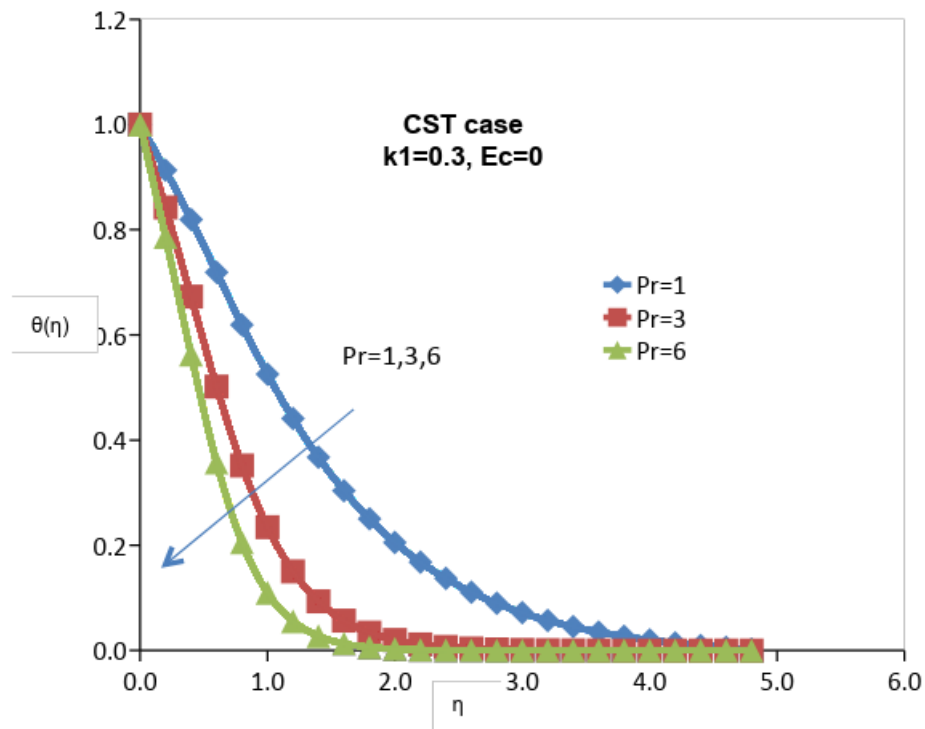
Fig 7(a) and Fig 7(b) depict the effect of viscoelastic parameter k_1 on longitudinal and transverse velocity components. It can be seen, for a fixed value of η , both $f'(\eta)$ and $f(\eta)$ decrease with increasing values of viscoelastic parameter k_1 . This can be explained by the fact that, as the viscoelastic parameter k_1 increases, the boundary layer adheres strongly to the surface, which in turn retards the flow in longitudinal and transverse directions.

Fig 8(a) and 8(b) show the effect of Magnetic field parameter on temperature distribution in PST and PHF cases respectively. Temperature profile increases with increase in magnetic field. Since increase of magnetic field increases the thermal boundary layer thickness. The increasing frictional drag due to Lorentz force is responsible for increasing the thermal boundary layer thickness.

VI. CONCLUSIONS:

From our numerical results, it can be concluded that:

- i. Horizontal velocity profile decreases with increase in magnetic field parameter (Mn).
- ii. Temperature profiles increases with increase in magnetic field parameter (Mn).
- iii. Thermal boundary layer thickness decreases with increase in Prandtl number (Pr).
- iv. Work done deformation term in energy equation reduces the temperature profiles, this is in contrast to the second grade fluids.



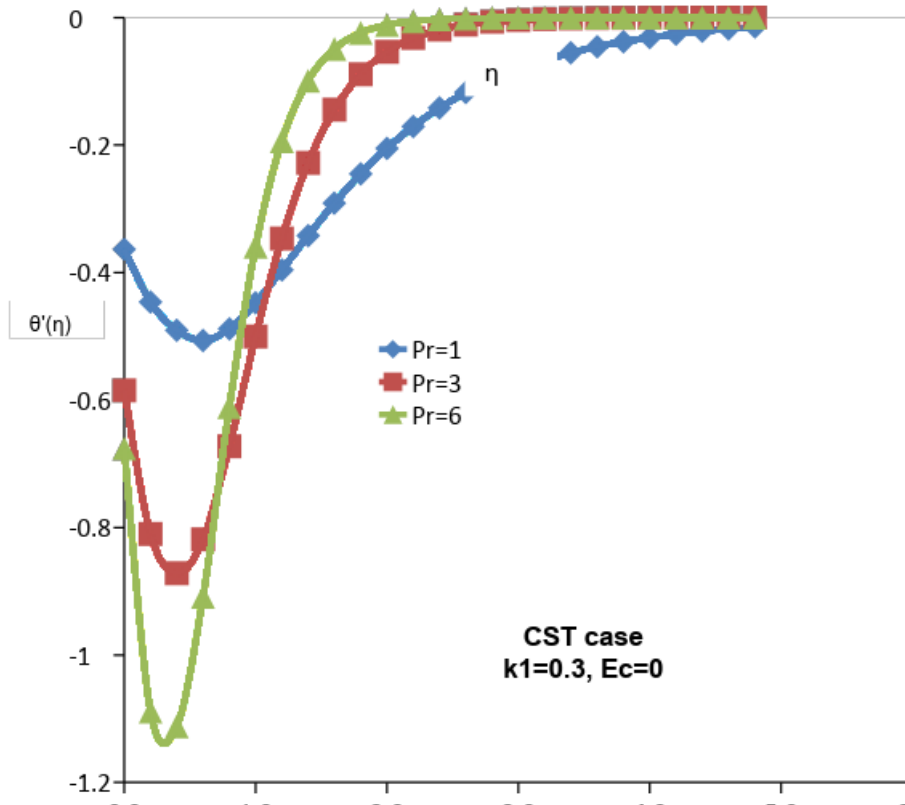
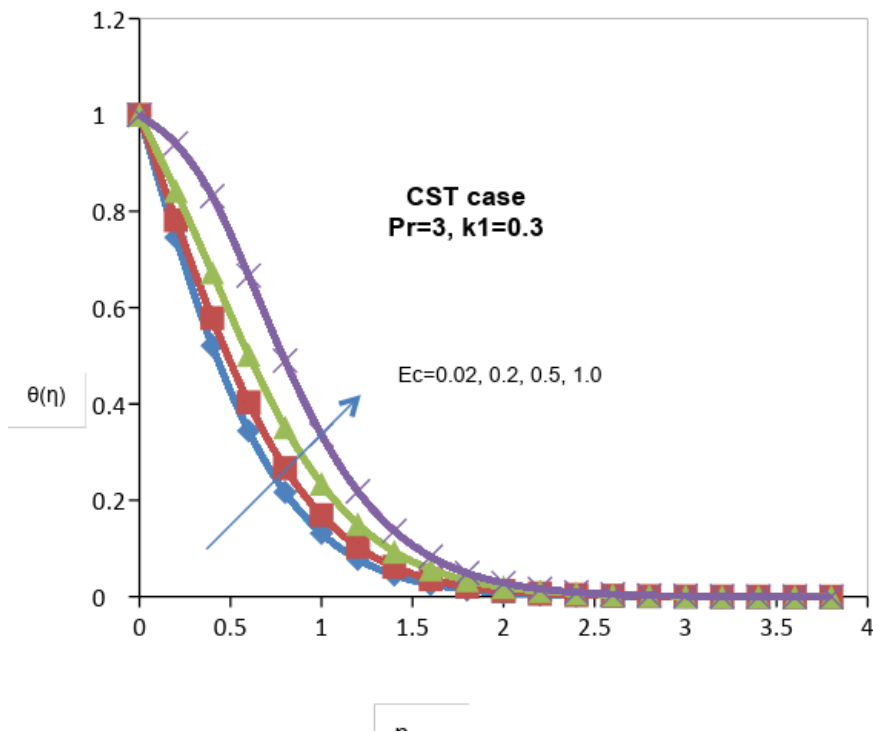


Fig.1. Effect of Prandtl number (Pr) on (a) Temperature $\theta(\eta)$ (b) Temperature gradient $\theta'(\eta)$ in CST case with $k_1=0.3, Ec=0$



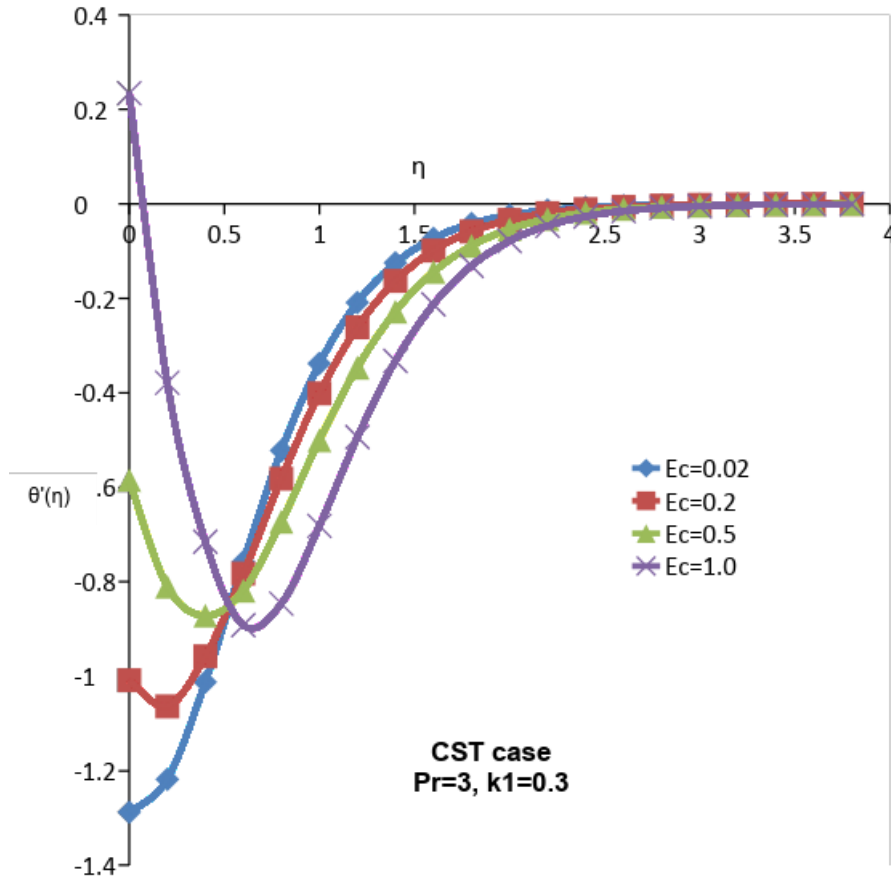


Fig 2. Effect of Eckert number (Ec) on (a) Temperature $\theta(\eta)$ (b) Temperature gradient $\theta'(\eta)$ in CST case with Pr=3, $k_1=0.3$

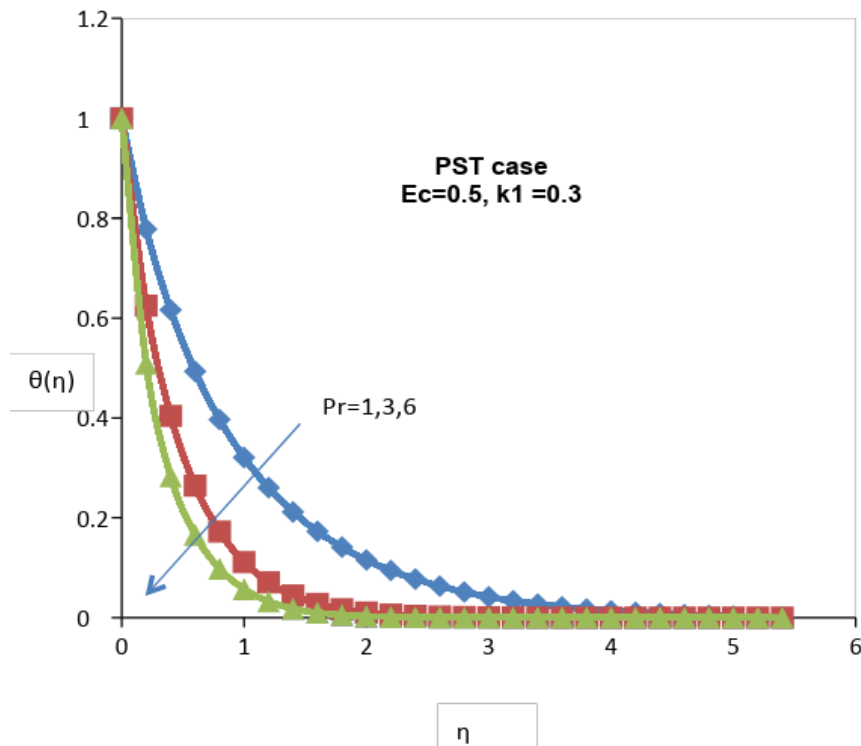


Fig 3. Effect of Prandtl number on Temperature profiles .

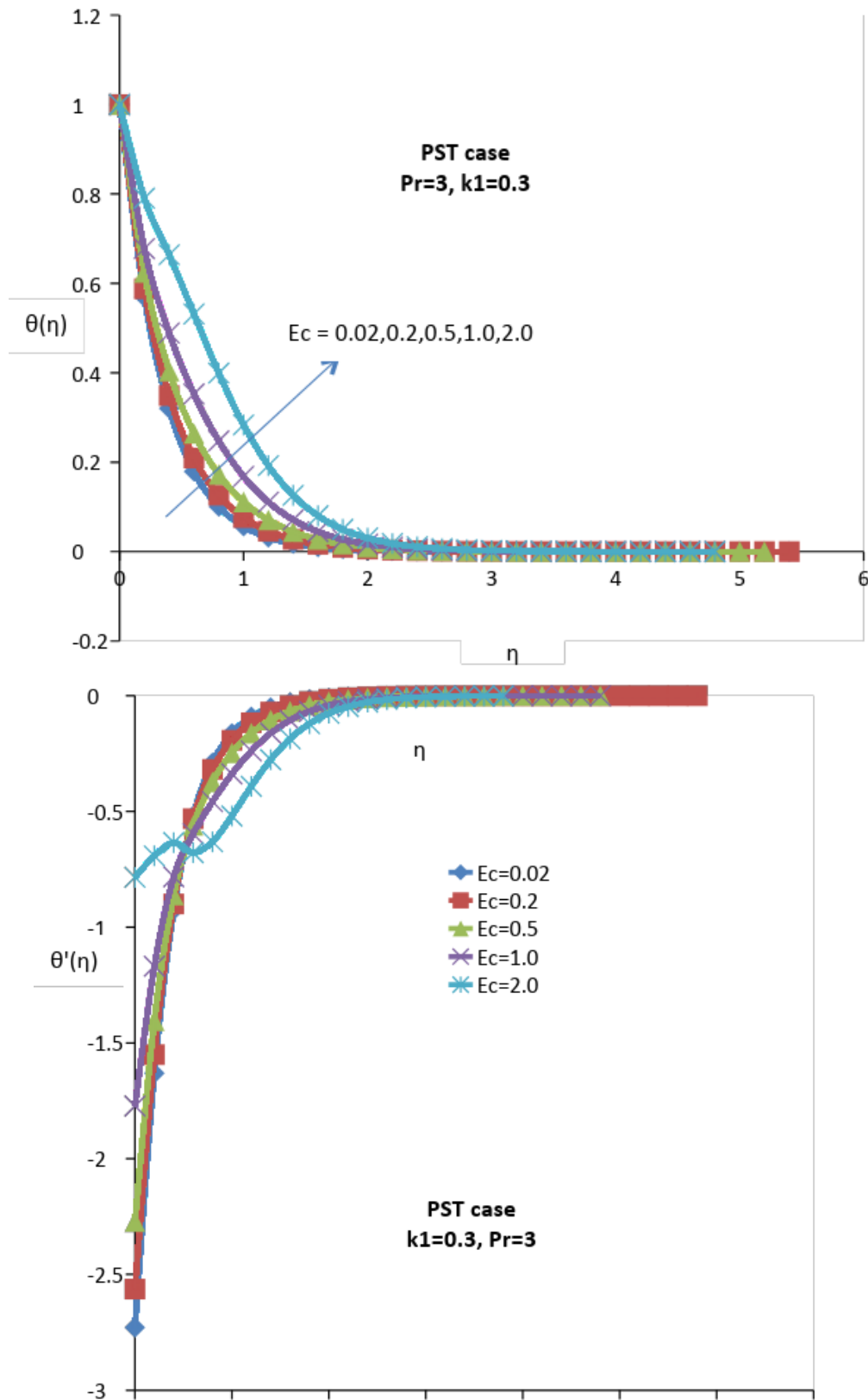


Fig 4. Effect of Eckert number (Ec) on (a) Temperature $\theta(\eta)$ (b) Temperature gradient $\theta'(\eta)$ in PST case with $Pr=3, k_1=0.3$

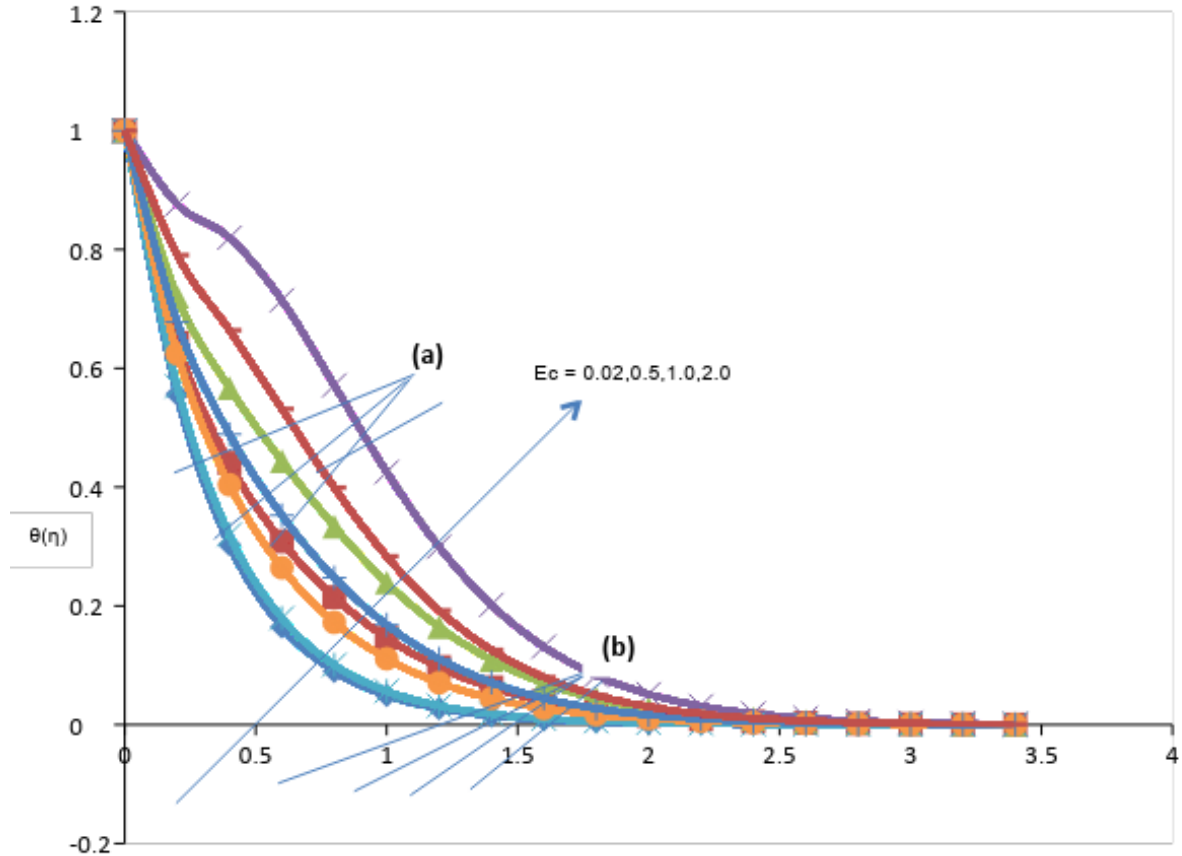


Fig 5. Temperature profiles for various values of Eckert number in PST case (a) without work due to deformation (b) with work due to deformation.

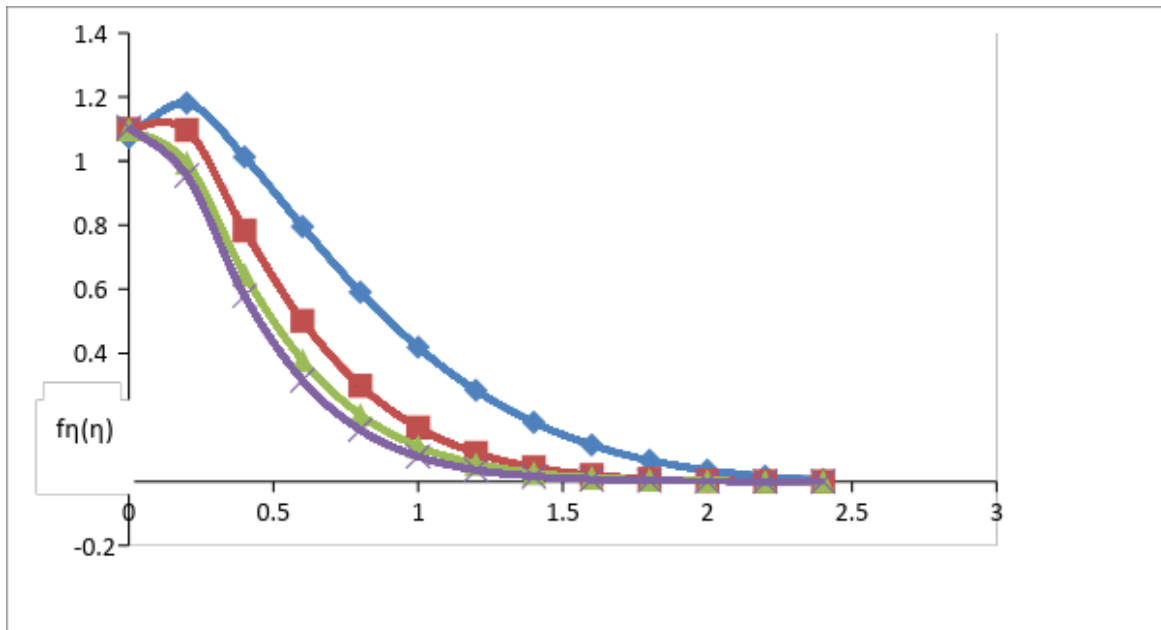


Fig6: Plot of velocity ($f_{\eta}(\eta)$) vs η for different values of Magnetic parameter (Mn)

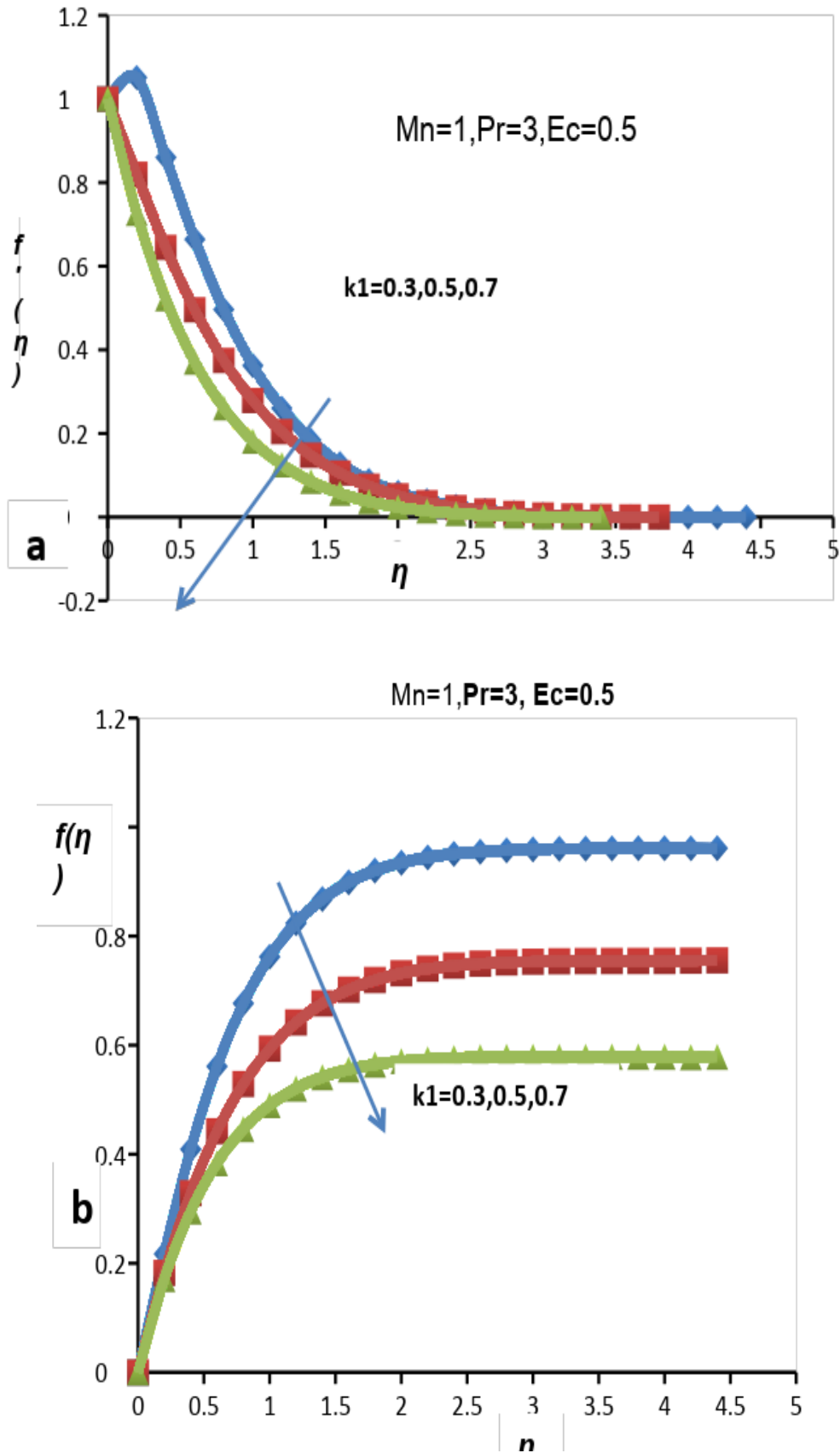


Fig7: Effect of viscoelasticity (k_1) on (a) transverse velocity component, (b) longitudinal component

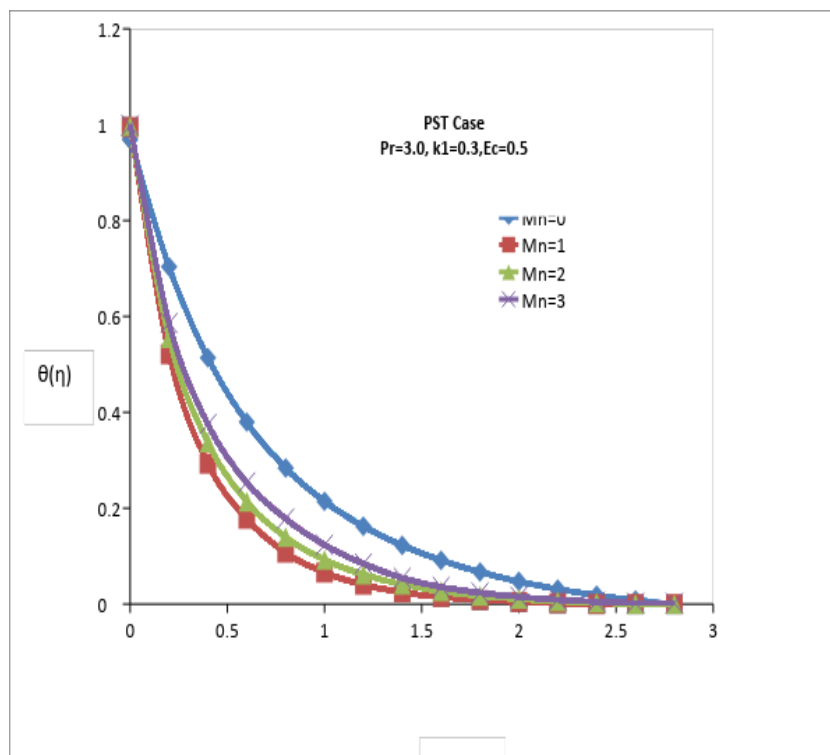


Fig 8. Effect of Magnetic field parameter (Mn) on temperature distribution $\theta(\eta)$

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